

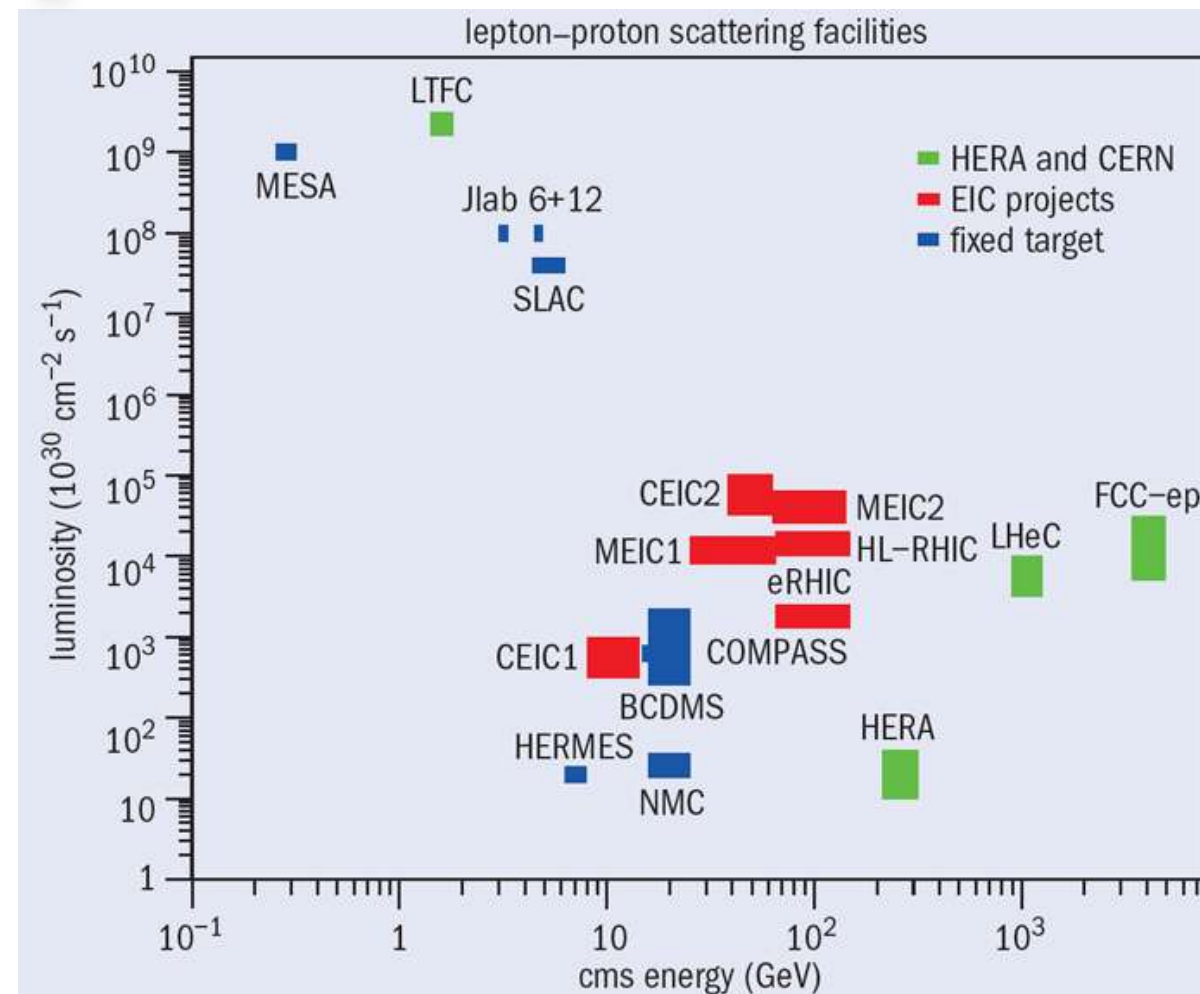
# Searching for parton saturation at FCC-eh, LHeC and EIC

*Open questions and path forward*

Anna Staśto



# Past, present and future of DIS



## US EIC

energy  $\sqrt{s} \simeq 20 - 140 \text{ GeV}$

luminosity  $10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

wide range of nuclei: p, d,  $^3\text{He}$ ,  $^4\text{He}$ , C, Ca, Cu, Au

polarization of electron and nucleon beams

## LHeC /FCC-ep (CERN)

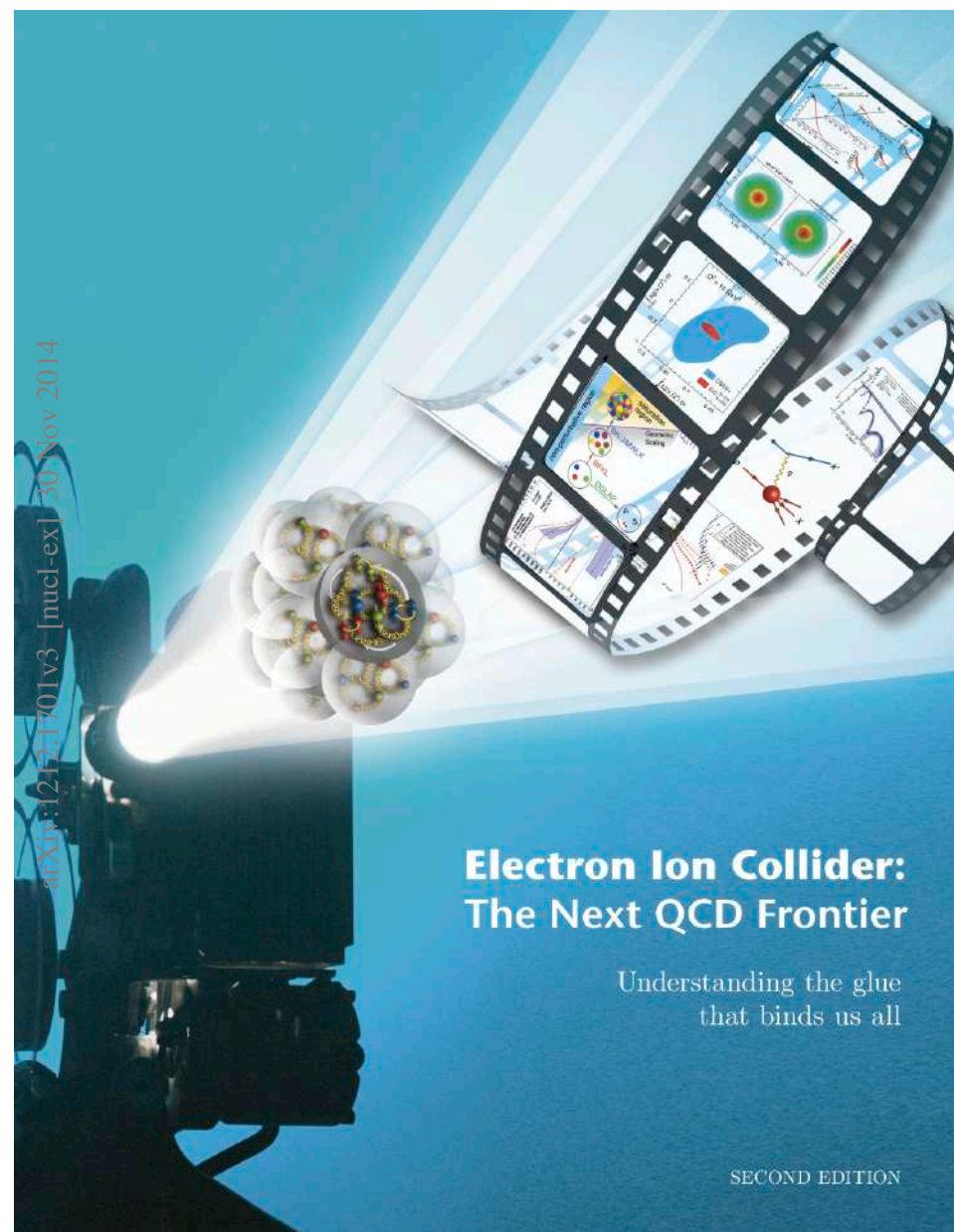
energy  $\sqrt{s} \simeq 1 - 5 \text{ TeV}$

luminosity  $10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

electron proton/ion: p, Pb

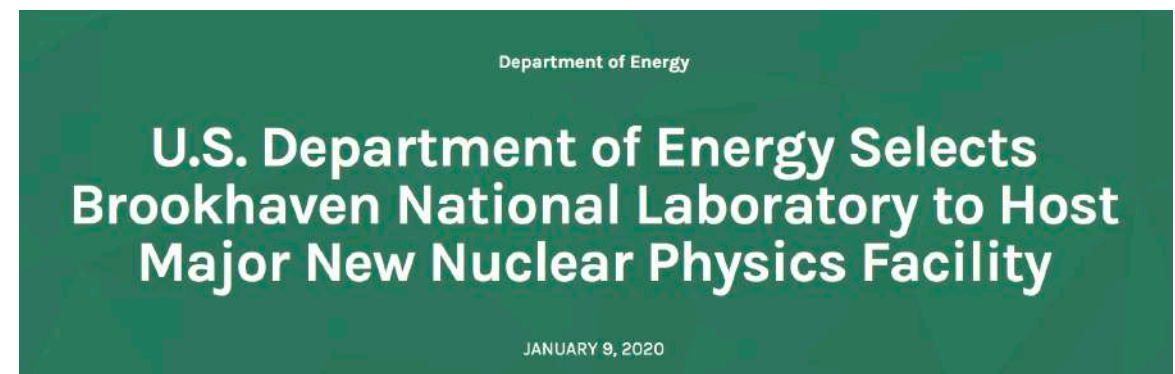
# Physics at high densities at the EIC

## 2012: EIC White Paper



## Chapter on high gluon density in QCD

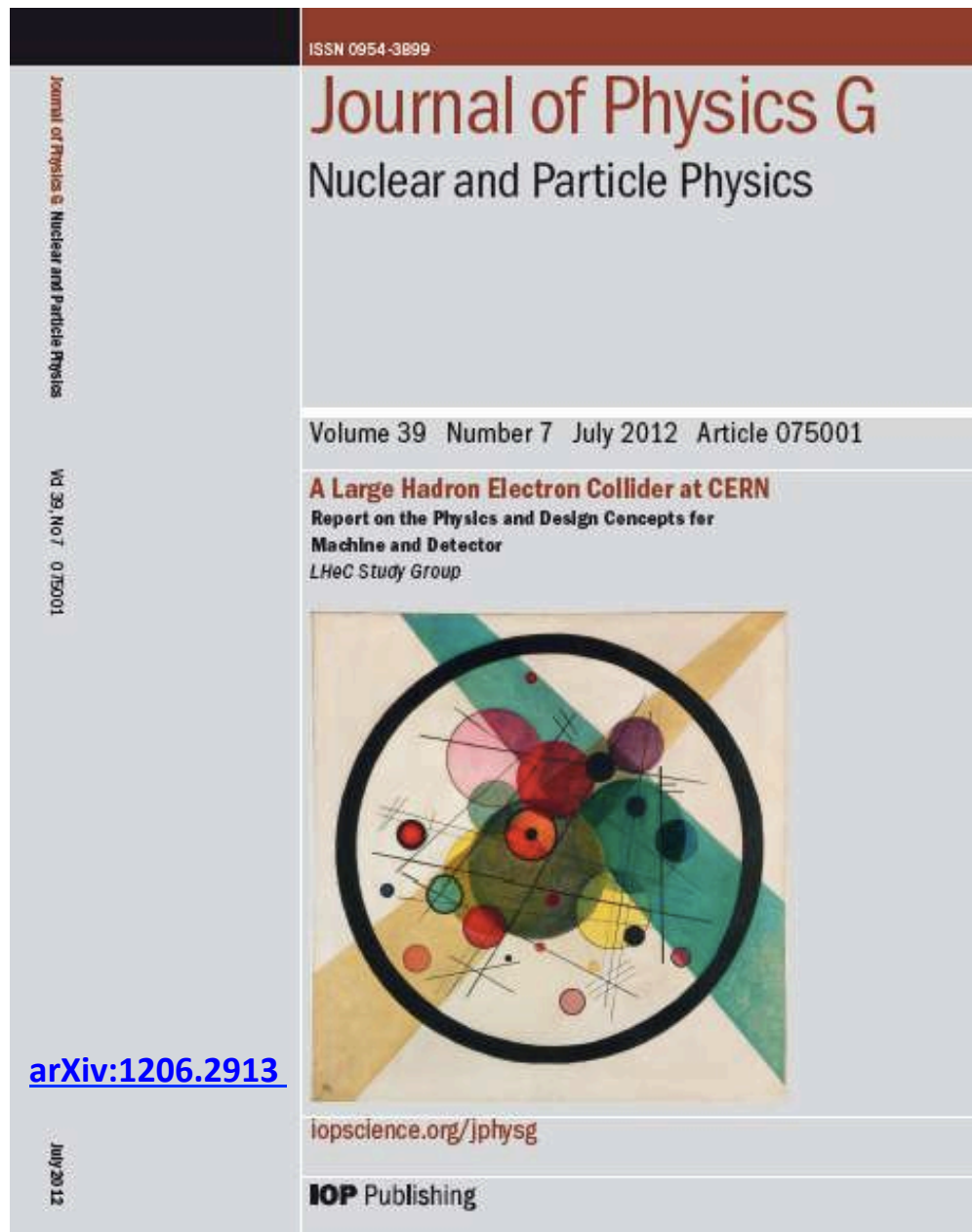
<b>3</b>	<b>The Nucleus: A Laboratory for QCD</b>	<b>57</b>
3.1	Introduction . . . . .	57
3.2	Physics of High Gluon Densities in Nuclei . . . . .	62
3.2.1	Gluon Saturation: a New Regime of QCD . . . . .	62
	Non-linear Evolution . . . . .	62
	Classical Gluon Fields and the Nuclear “Oomph” Factor . . . . .	65
	Map of High Energy QCD and the Saturation Scale . . . . .	67
	Nuclear Structure Functions . . . . .	69
	Diffractive Physics . . . . .	72
3.2.2	Key Measurements . . . . .	74
	Structure Functions . . . . .	76
	Di-Hadron Correlations . . . . .	80
	Measurements of Diffractive Events . . . . .	83



**2020/2021 Effort towards  
the Yellow Report: Physics/Detector  
development.**

# Physics at high densities at the LHeC

## 2012: LHeC Conceptual Design Study



**LHeC:** Large Hadron electron Collider. CERN Project to collide electrons with LHC proton/ion beam

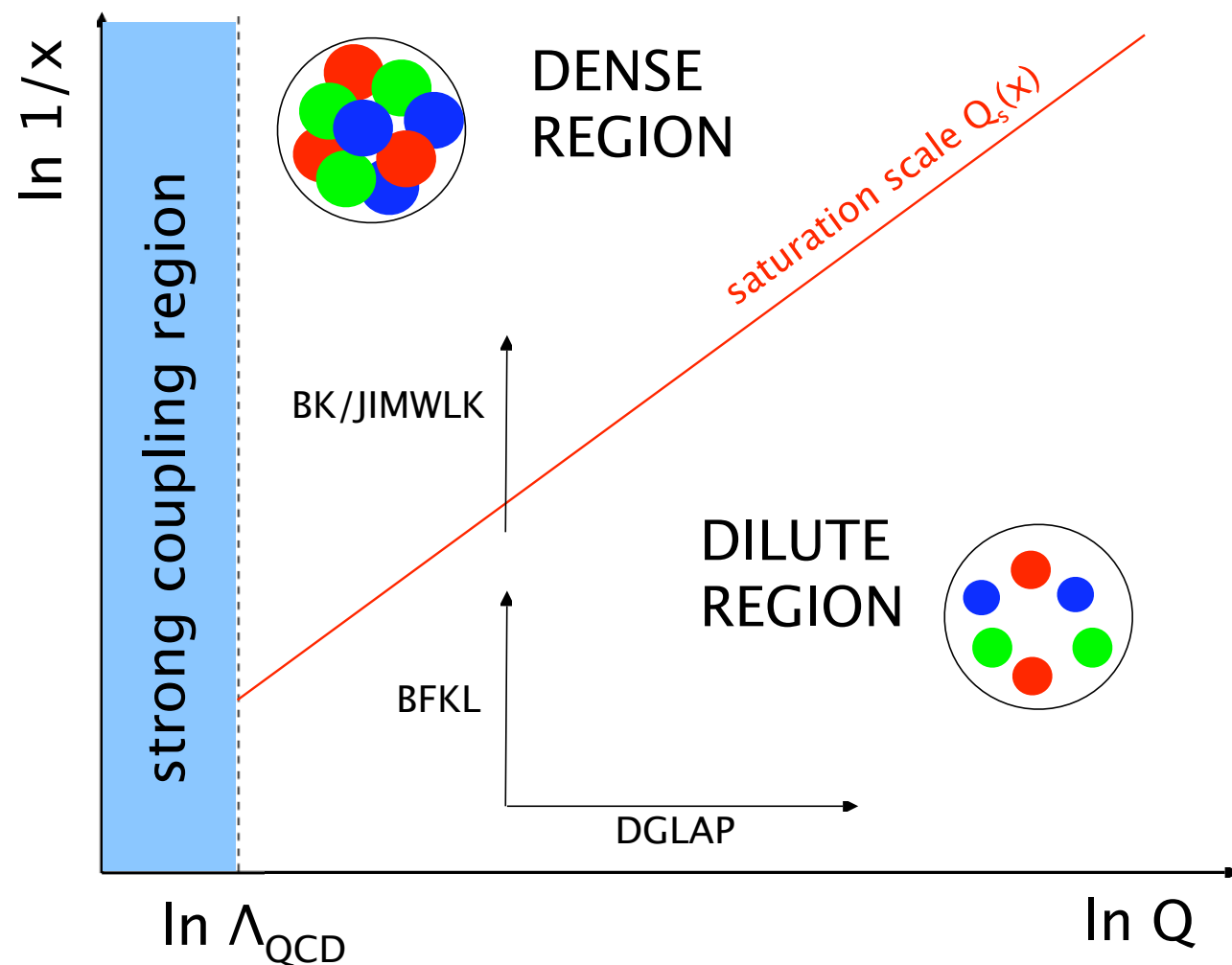
### 6 Physics at High Parton Densities

- 6.1 Physics at small  $x$  . . . . .
  - 6.1.1 High energy and density regime of QCD . . . . .
  - 6.1.2 Status following HERA data . . . . .
  - 6.1.3 Low- $x$  physics perspectives at the LHC . . . . .
  - 6.1.4 Nuclear targets . . . . .
- 6.2 Prospects at the LHeC . . . . .
  - 6.2.1 Strategy: decreasing  $x$  and increasing  $A$  . . . . .
  - 6.2.2 Inclusive measurements . . . . .
  - 6.2.3 Exclusive Production . . . . .
  - 6.2.4 Inclusive diffraction . . . . .
  - 6.2.5 Jet and multi-jet observables, parton dynamics and fragmentation . . . . .
  - 6.2.6 Implications for ultra-high energy neutrino interactions and detection . . . . .

2020 update of the  
CDR to be released soon (July 2020)



# Transition regime to high parton density



$x$  and  $A$  dependent **saturation** scale.

$$\frac{A \times xg(x, Q_s^2)}{\pi A^{2/3}} \times \frac{\alpha_s(Q_s^2)}{Q_s^2} \sim 1$$

$$Q_s^2 \sim A^{1/3} Q_0^2 \left( \frac{1}{x} \right)^\lambda$$

Saturation boundary needs to be determined by experiment

HERA data consistent with very low  $Q_s$   
Partonic/perturbative interpretation uncertain

$$Q_s^2 \leq 1 \text{ GeV}^2$$

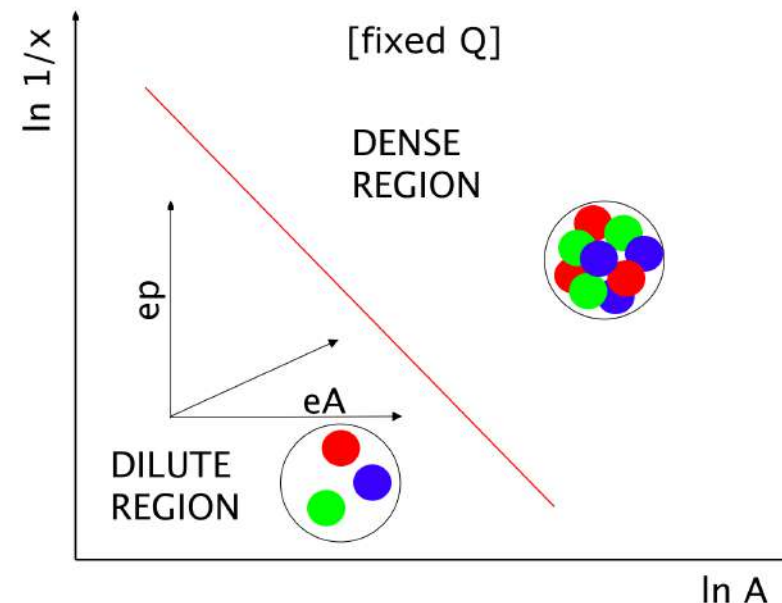
Gluon density can increase by: **decreasing  $x$**  and/or **increasing  $A$**

# Strategy for making target more 'black'

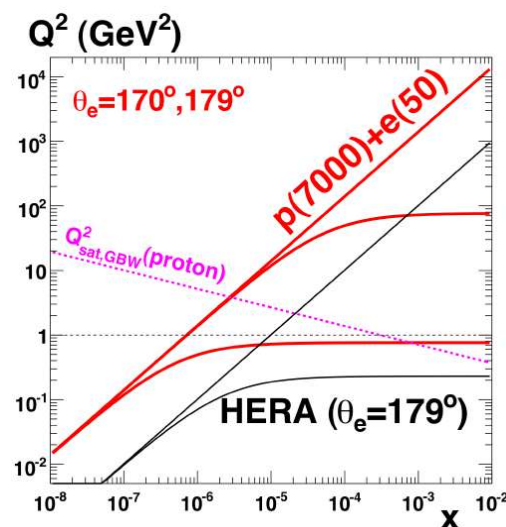
Saturation scale:  $Q_s^2 \sim A^{1/3} Q_0^2 \left( \frac{1}{x} \right)^\lambda$

Two-pronged approach

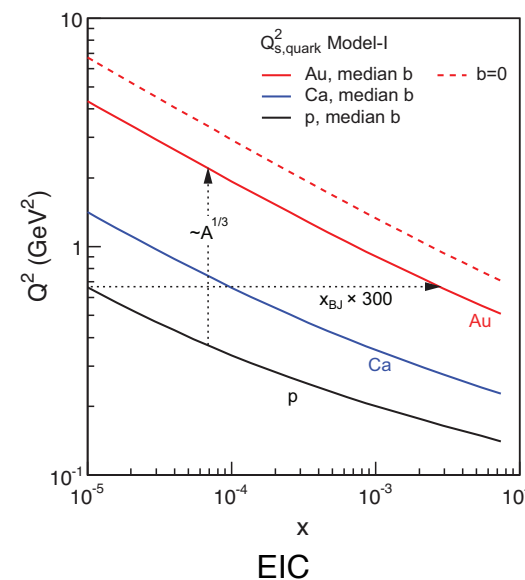
Probing lower x in ep.  
Evolution of a single  
source



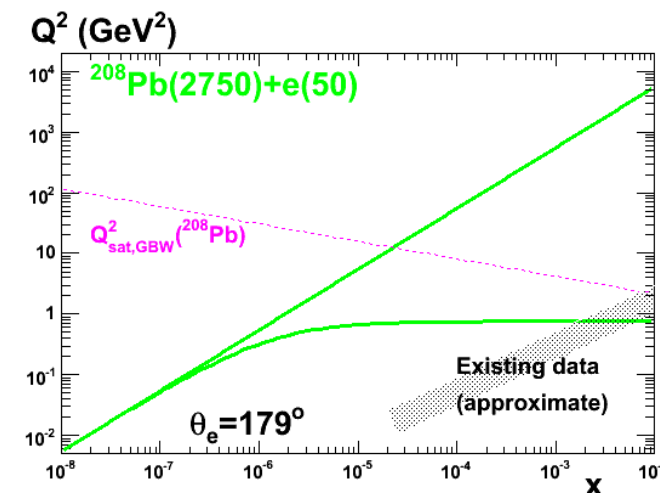
eA scattering  
Many sources  
overlapping in impact  
parameter .



LHeC/FCC-ep

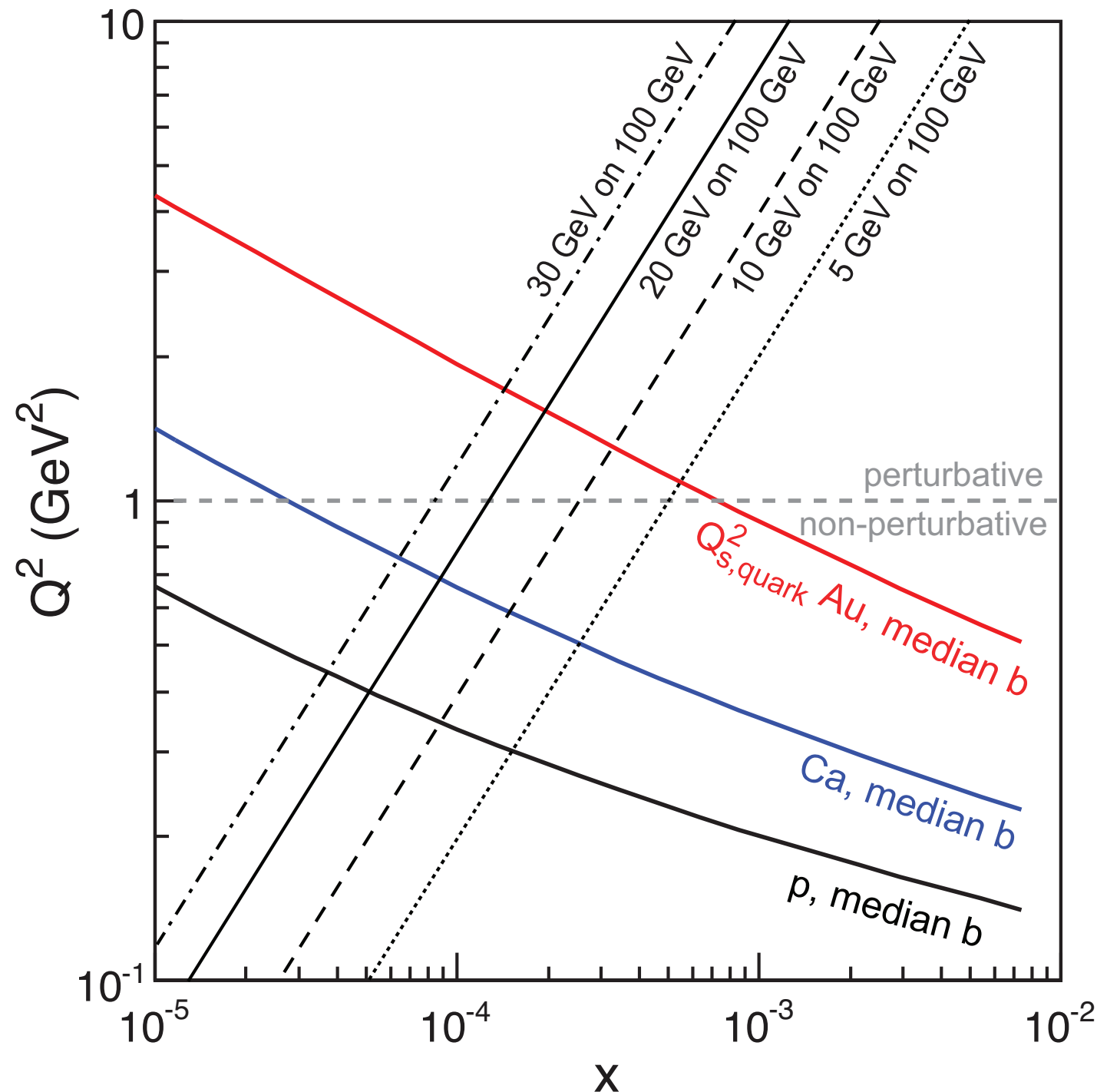


EIC



LHeC/FCC-eA

# EIC sensitivity to saturation scale



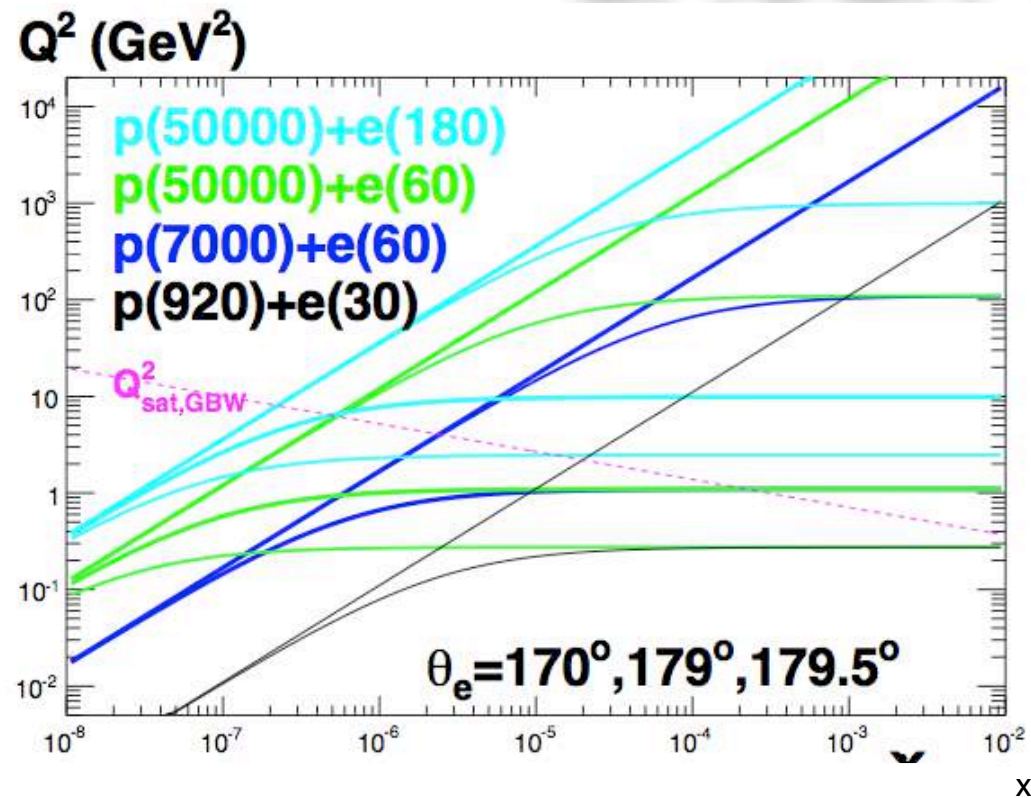
$$Q_s^2 \sim A^{1/3} Q_0^2 \left( \frac{1}{x} \right)^\lambda$$

EIC sensitive to perturbative saturation region in scattering with heavy nuclei.

Shown: median  $b$ -impact parameter.

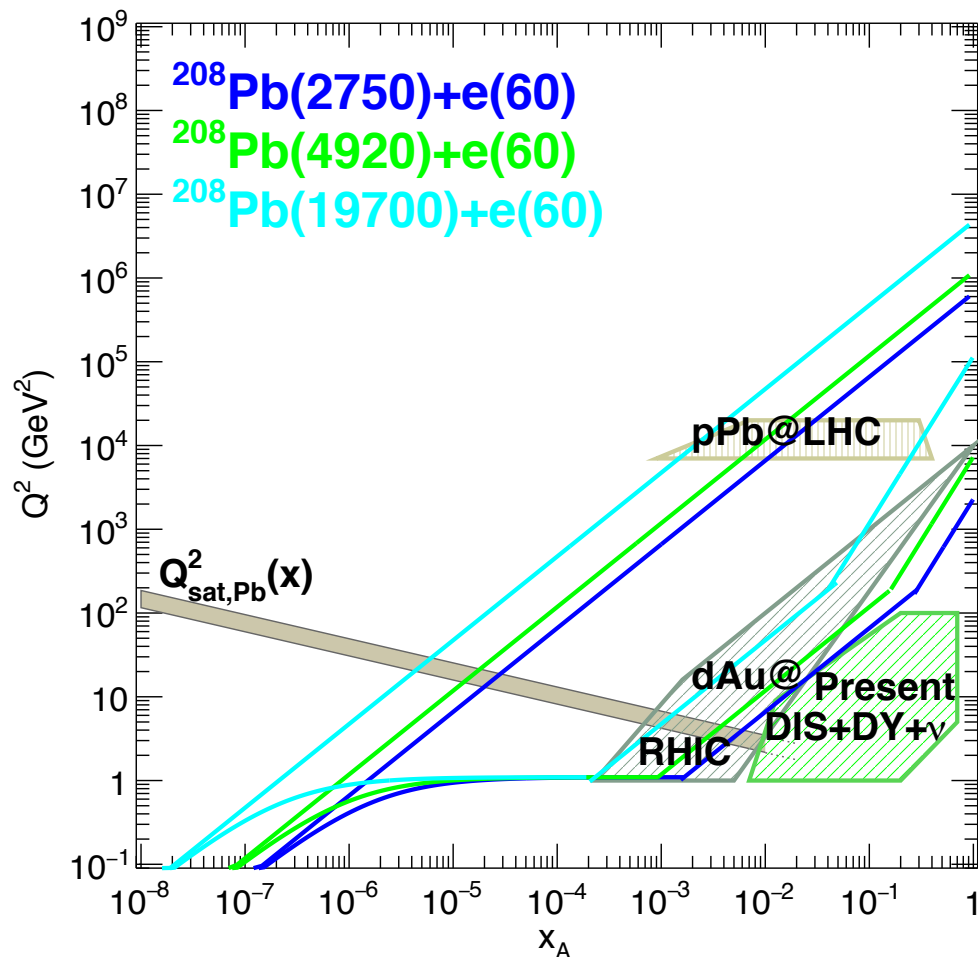
Exclusive processes can be sensitive to different  $b$ .

# LHeC/FCC-eh kinematics



LHeC/FCC-eh: Small  $x$  machines. Obvious extension of the kinematic reach at FCC- (electron-hadron)

Higher electron energy reduces small  $x$  region unless detector acceptance is larger.

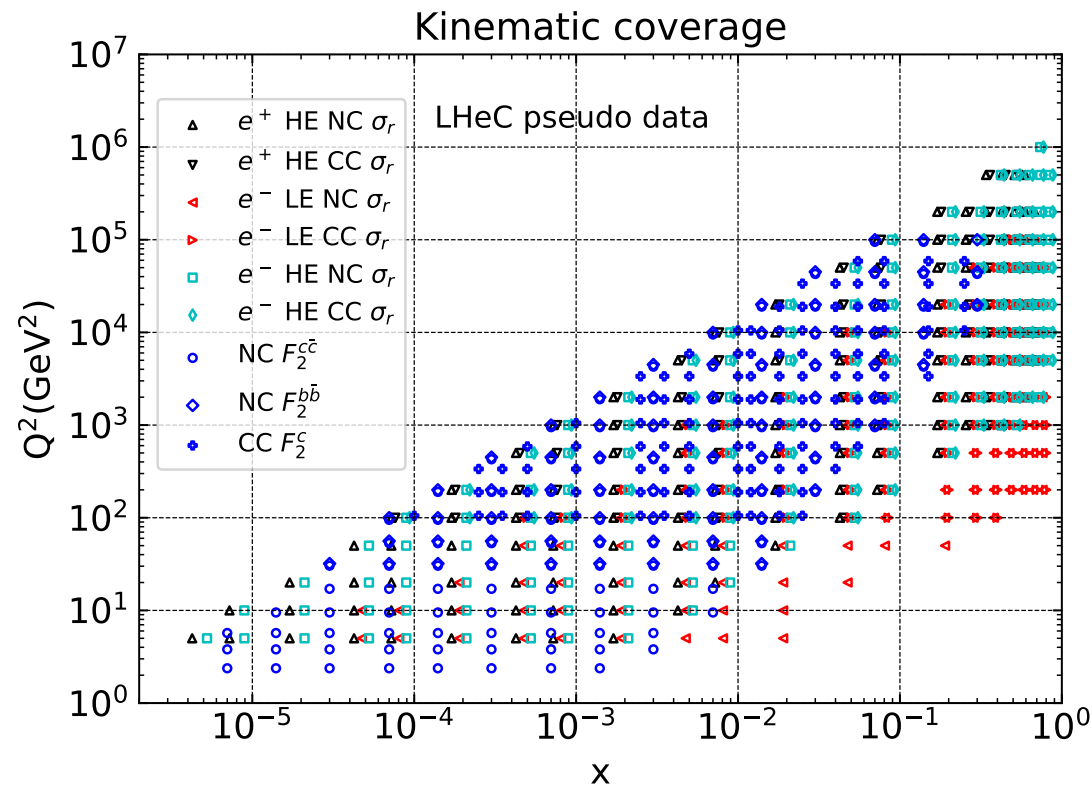


Similarly for eA mode: very small  $x$  domain in eA.

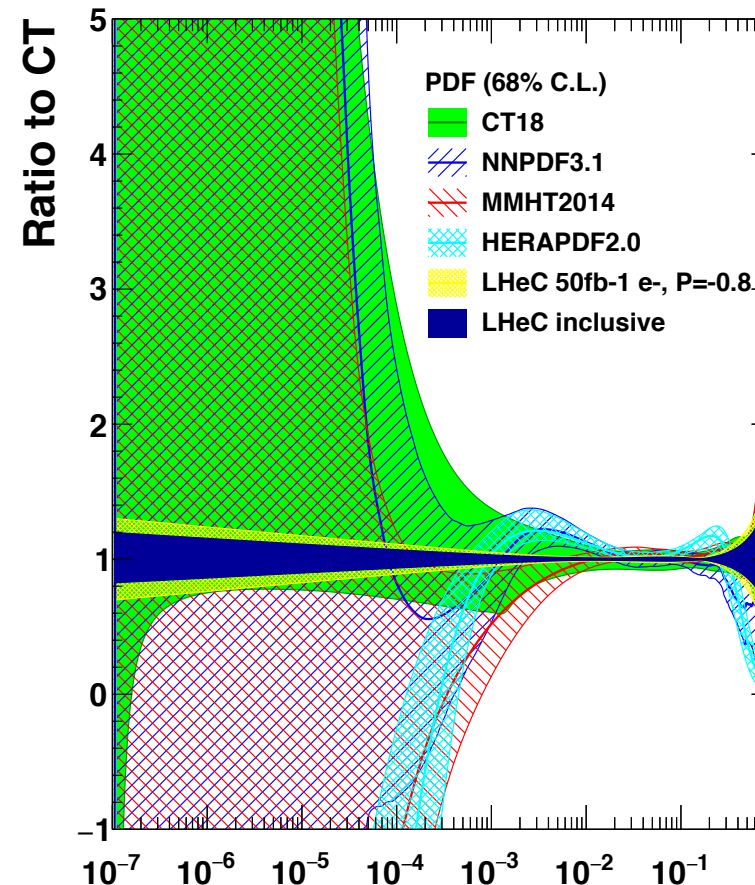


# LHeC constraints on gluon

Pseudodata

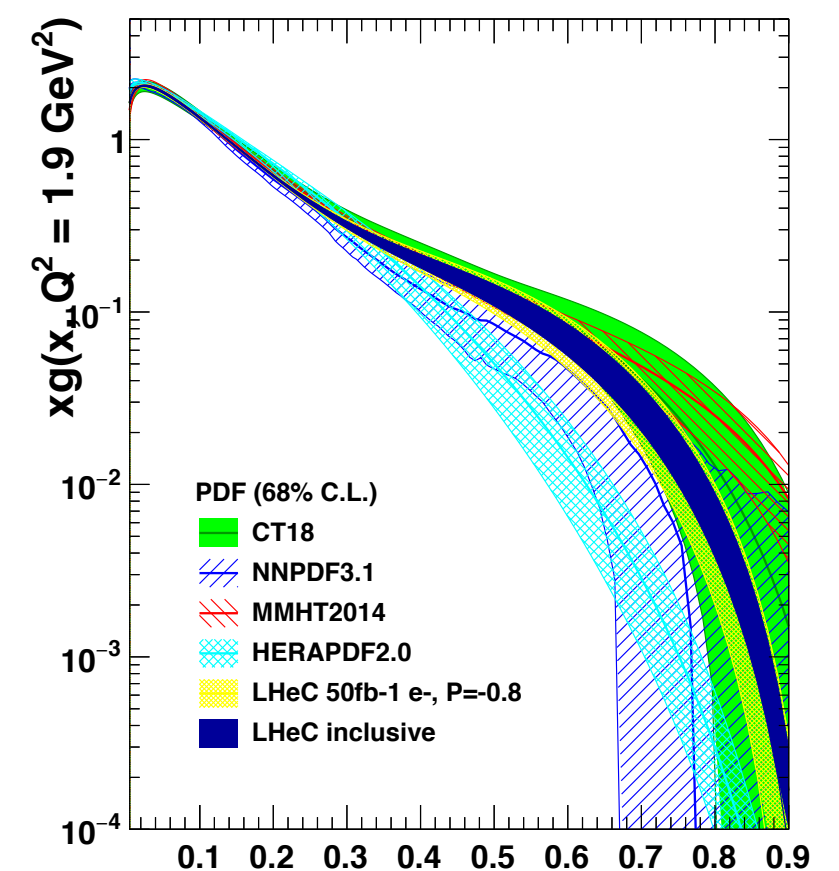


gluon distribution at  $Q^2 = 1.9 \text{ GeV}^2$



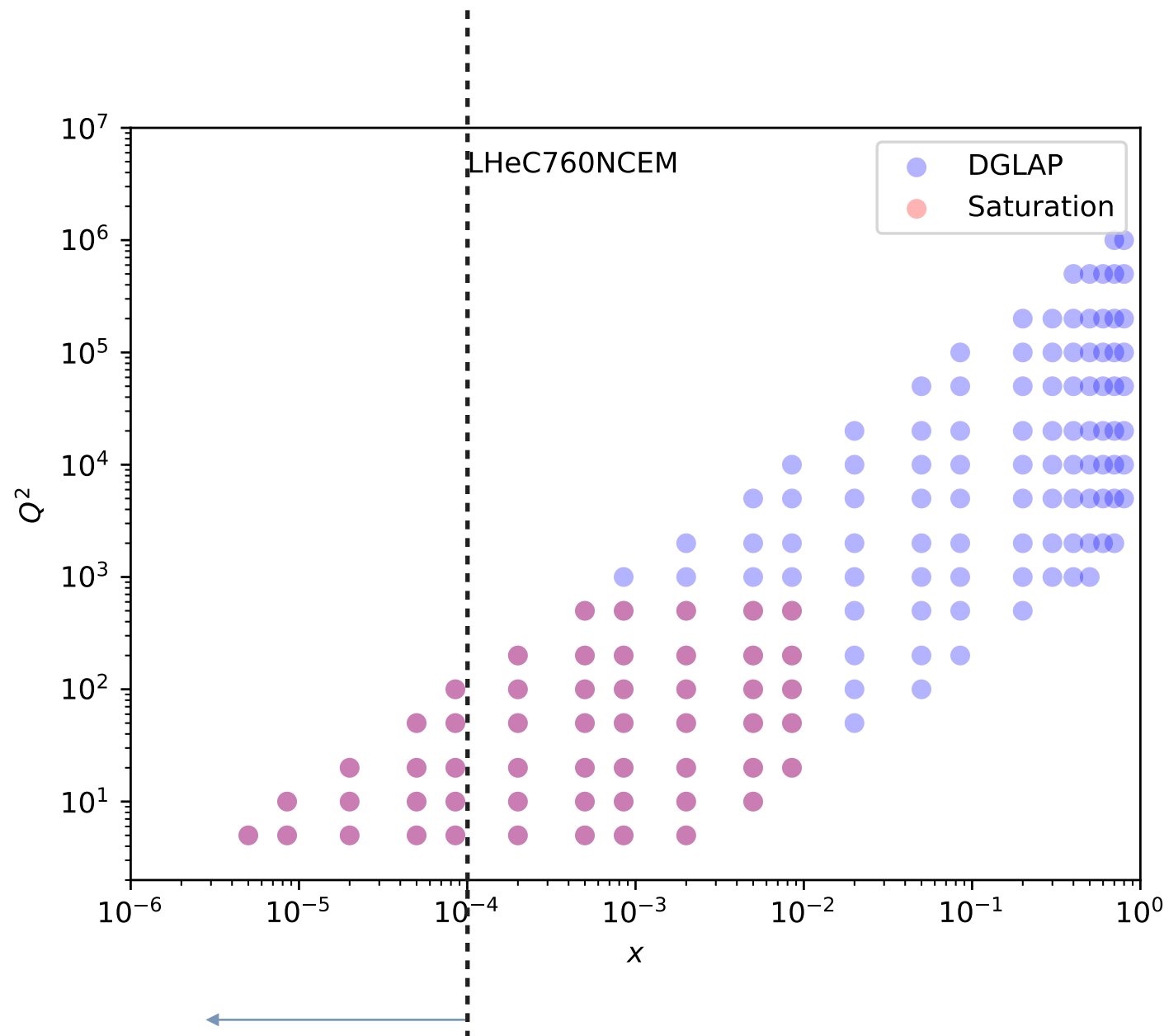
Constraints at both low  
and large  $x$

gluon distribution at  $Q^2 = 1.9 \text{ GeV}^2$



# Saturation: structure functions

Idea: generate pseudodata with/without saturation, fit with DGLAP and look for differences.



LHeC pseudodata: use two setups

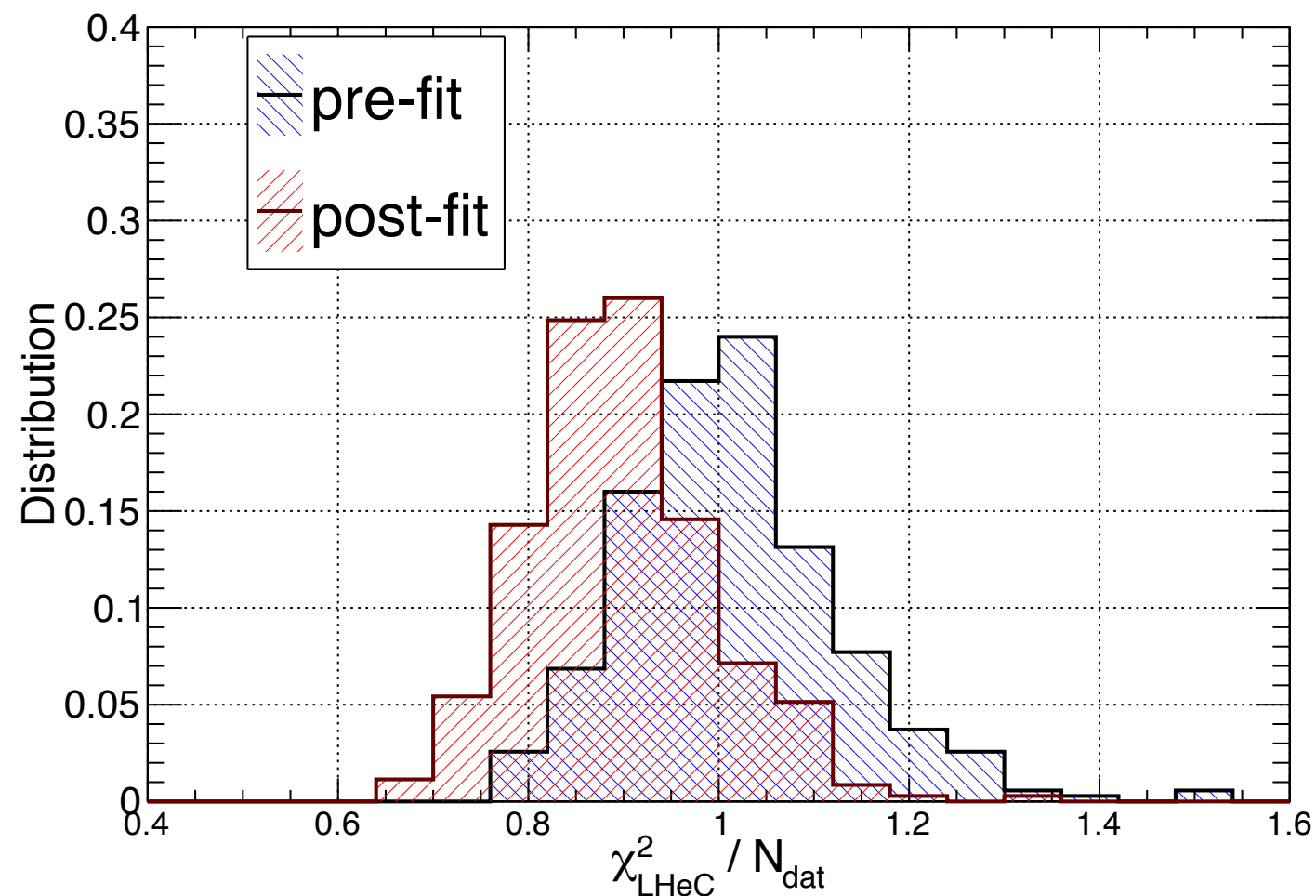
- DGLAP only (PDF4LHC15)
- DGLAP for  $x > 10^{-4}$  and saturation model for  $x < 10^{-4}$  (Golec-Biernat, Sapeta)

Method : Abdul Khalek, Bailey, Gao, Harland-Lang, Rojo. Hessian profiling.

Generated 500 independent sets of LHeC NC pseudodata with random fluctuations determined by (projected) experimental uncertainties.

# Saturation: structure functions

DGLAP-based LHeC pseudo-data (PDF4LHC15)



Distribution of pre-fit and post-fit values of

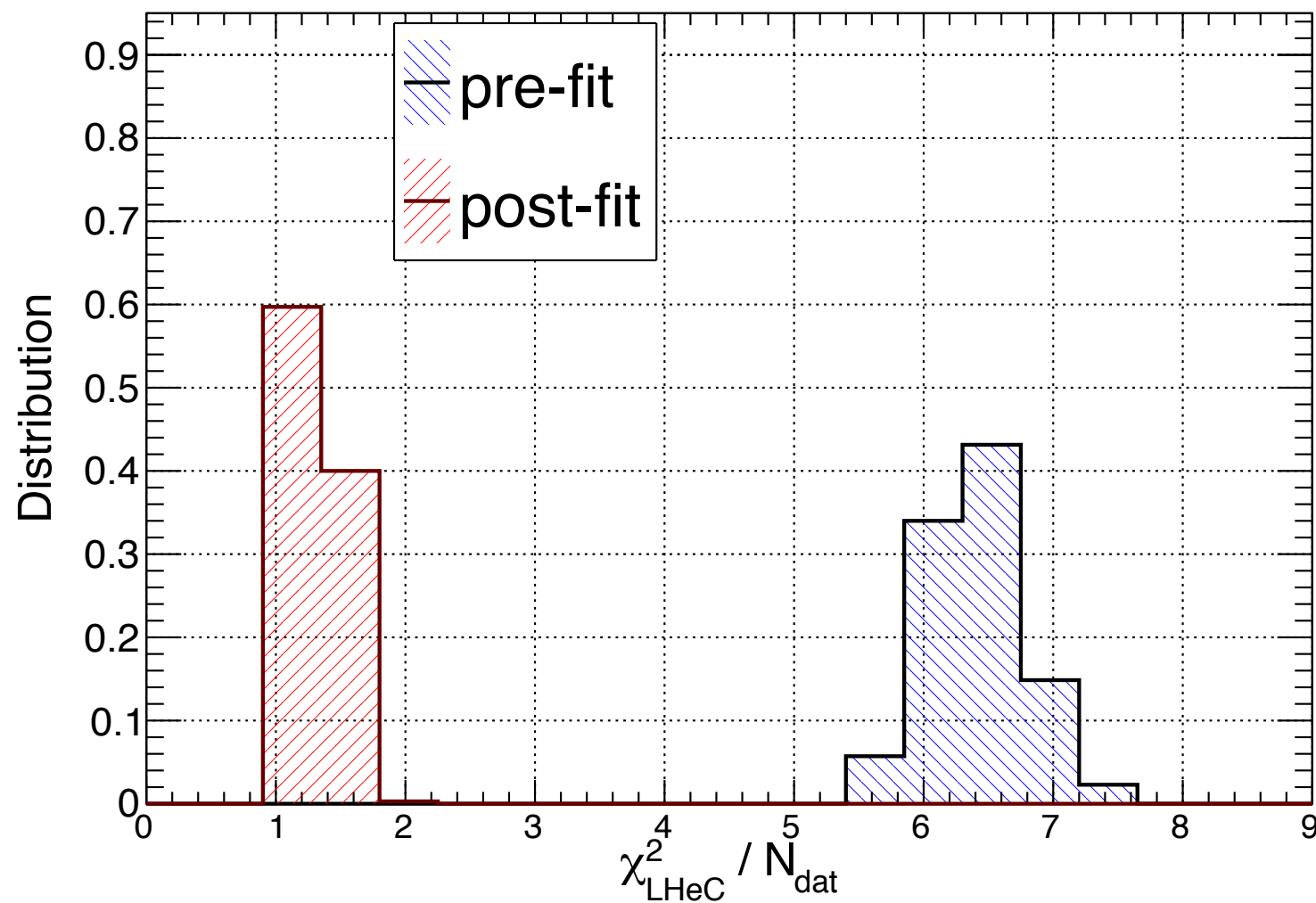
$$\chi^2 / n_{\text{dat}}$$

for 500 data sets.

Fit done with model used to generate pseudodata: very good agreement obviously...

# Saturation: structure functions

Saturation LHeC pseudo-data (for  $x < 10^{-4}$ )



LHeC data with saturation:

Pre-fit distribution: mean around 6.5

Post-fit distribution: mean much lower 1.3  
Seems like DGLAP can absorb saturation effects

But how much?



# Saturation: structure functions

Zoom into post-fit distribution

Can still tell apart between DGLAP and saturation pseudodata

DGLAP cannot completely fit away saturation effects, if they are present at LHeC below  $x < 10^{-4}$

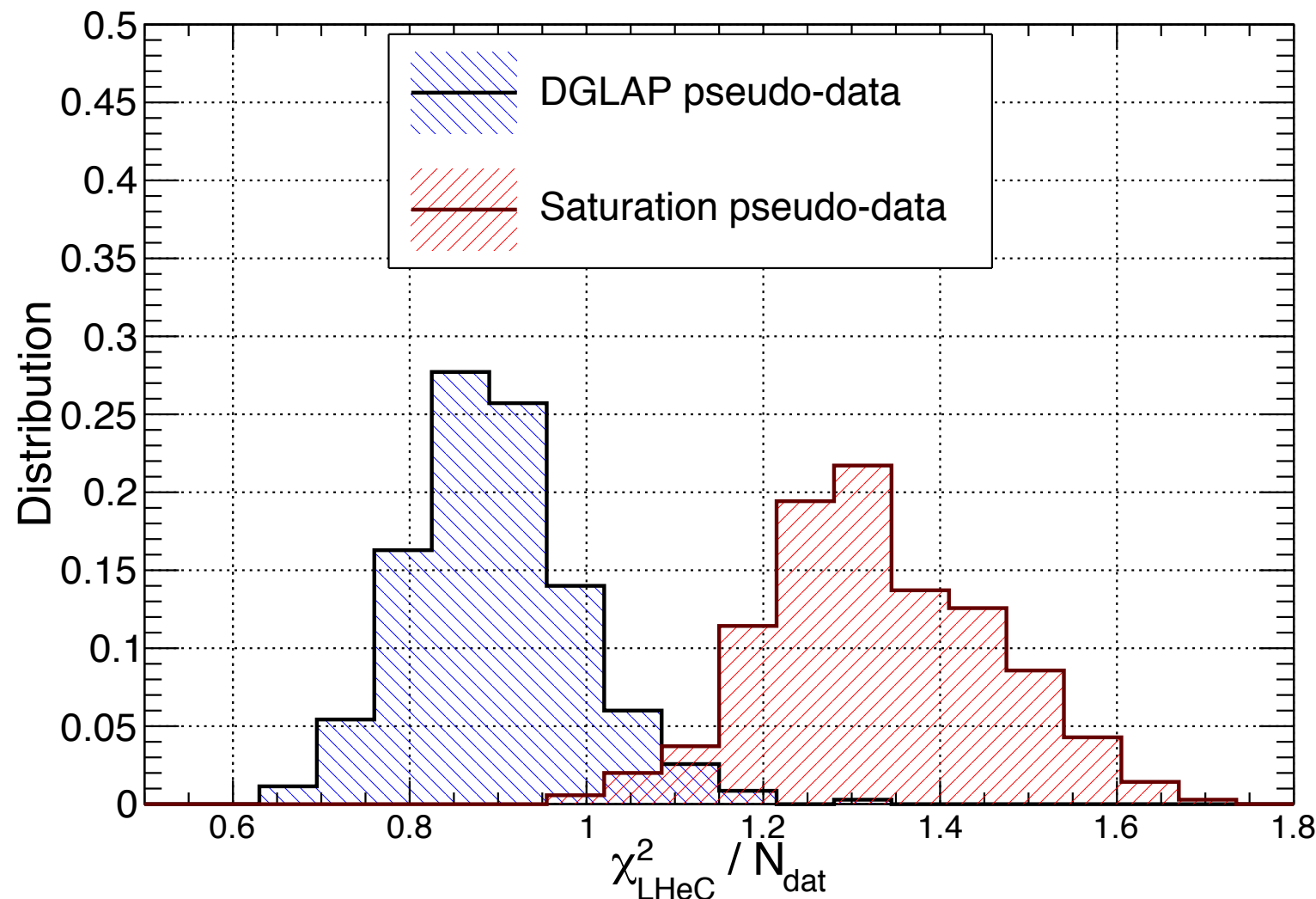
*Comments: will strongly depend on model and range of  $x$  and  $Q$  where the modifications are present*

*More pronounced at FCC*

*Can perform similar exercise with nuclear structure functions*

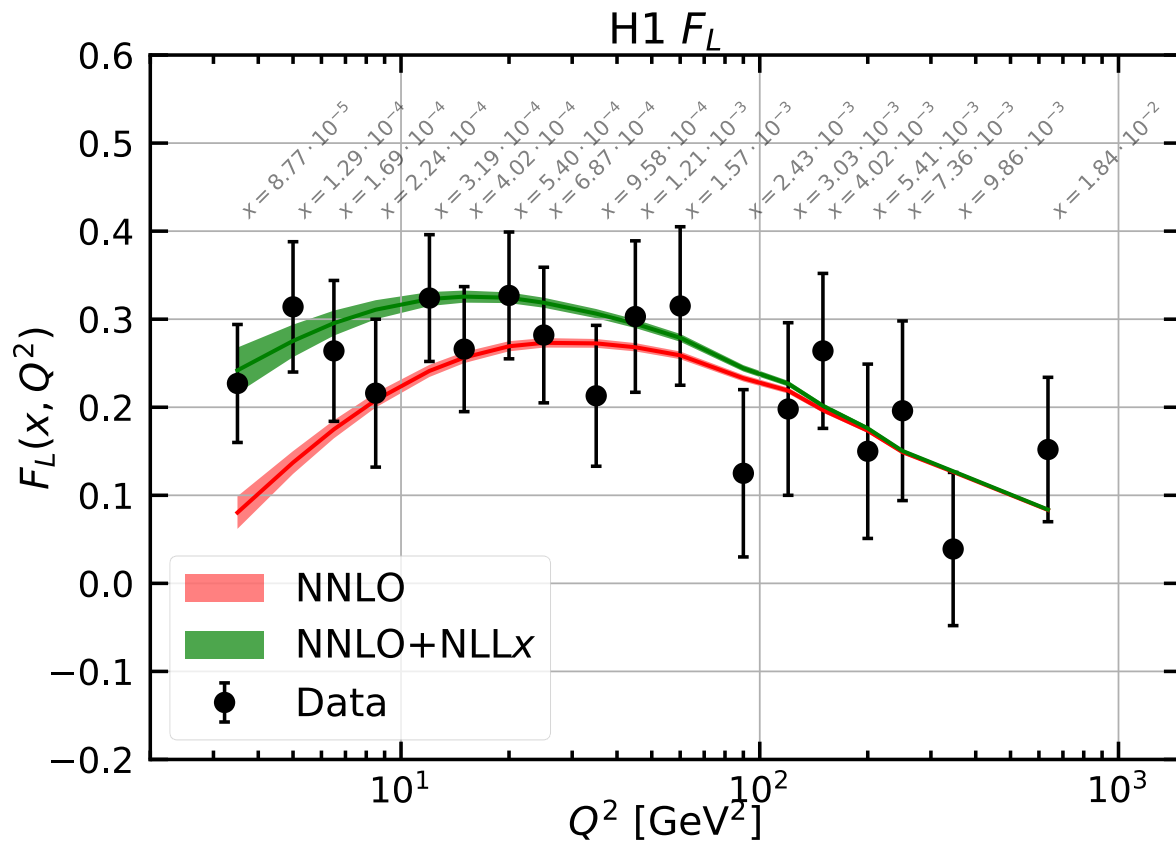
*Other observables: charm and longitudinal structure function*

Post-fit results to LHeC (500 pseudo-experiments)



# Longitudinal structure function

$$\frac{Q^4 x}{2\pi\alpha^2 Y_+} \cdot \frac{d^2\sigma}{dx dQ^2} = \sigma_r \simeq F_2(x, Q^2) - f(y) \cdot F_L(x, Q^2) = F_2 \cdot \left(1 - f(y) \frac{R}{1+R}\right) \quad y = Q^2/sx,$$



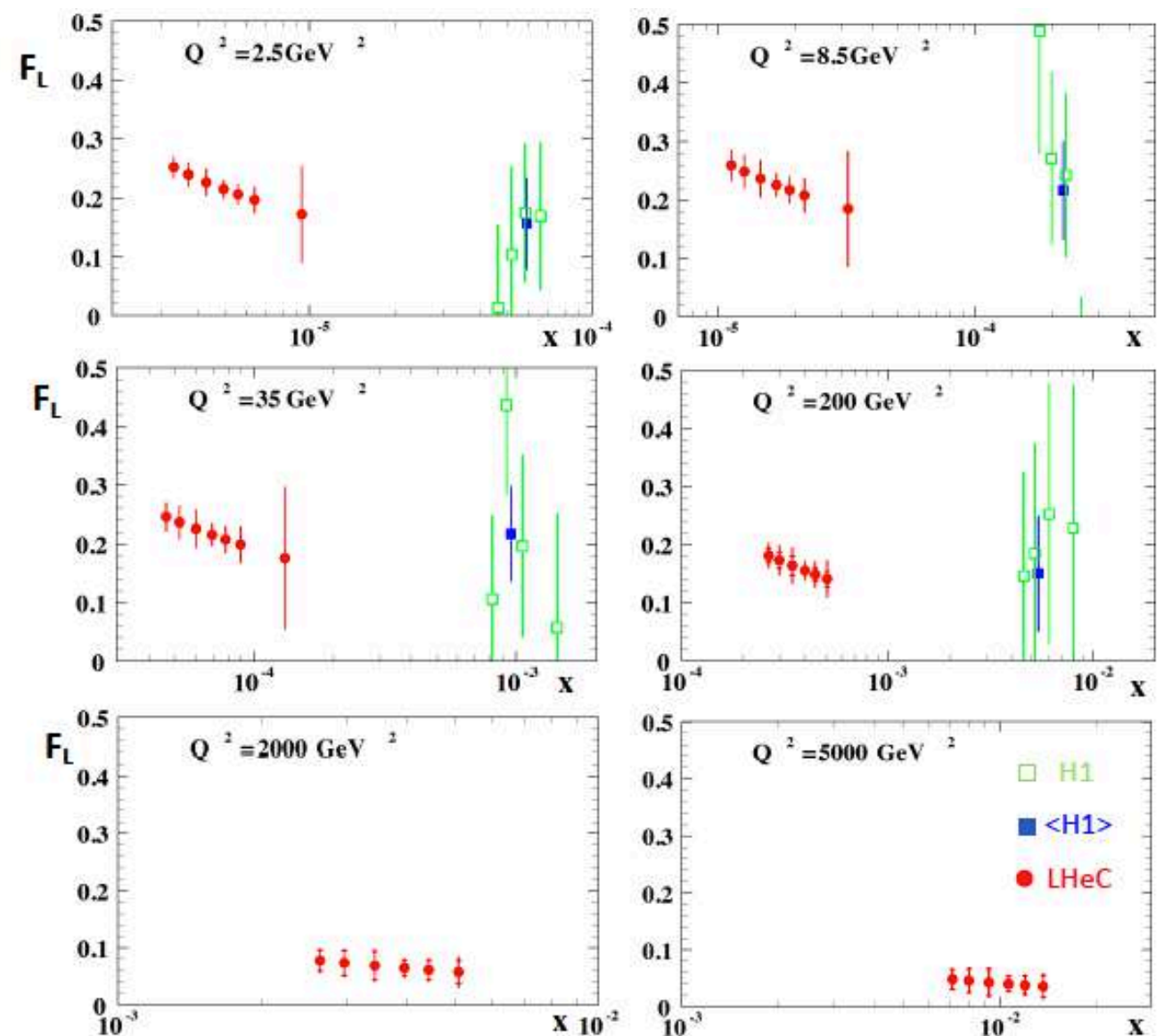
Longitudinal structure function: important constraint on the gluon

Challenging experimentally: vary energy,  $F_L$  small, systematics

$E_p=7$  TeV,  $E_e=60,30,20$  GeV

Luminosity: 10, 1, 1  $\text{fb}^{-1}$

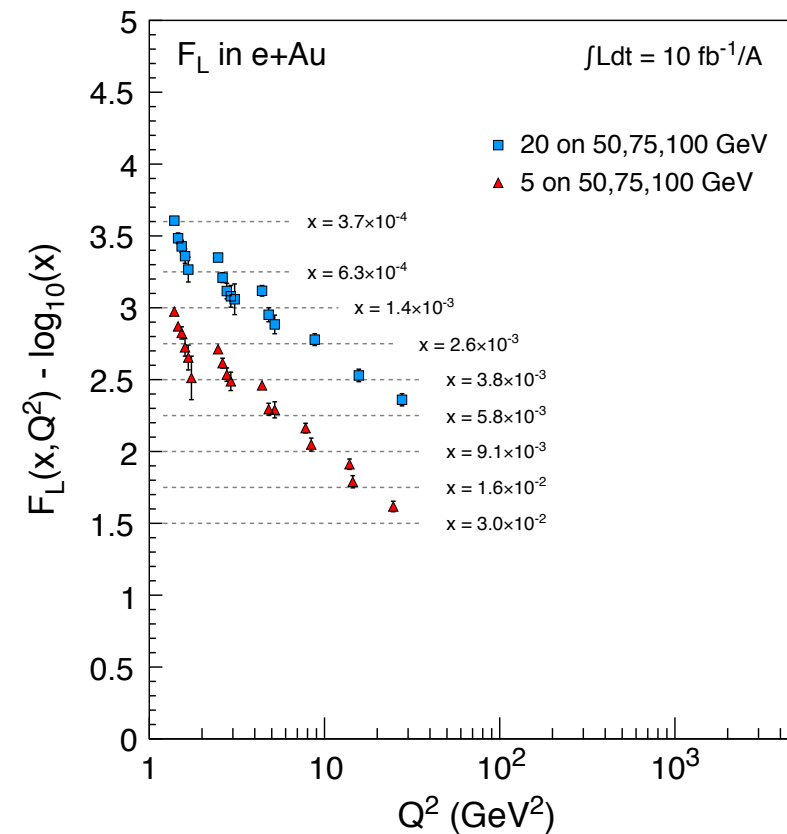
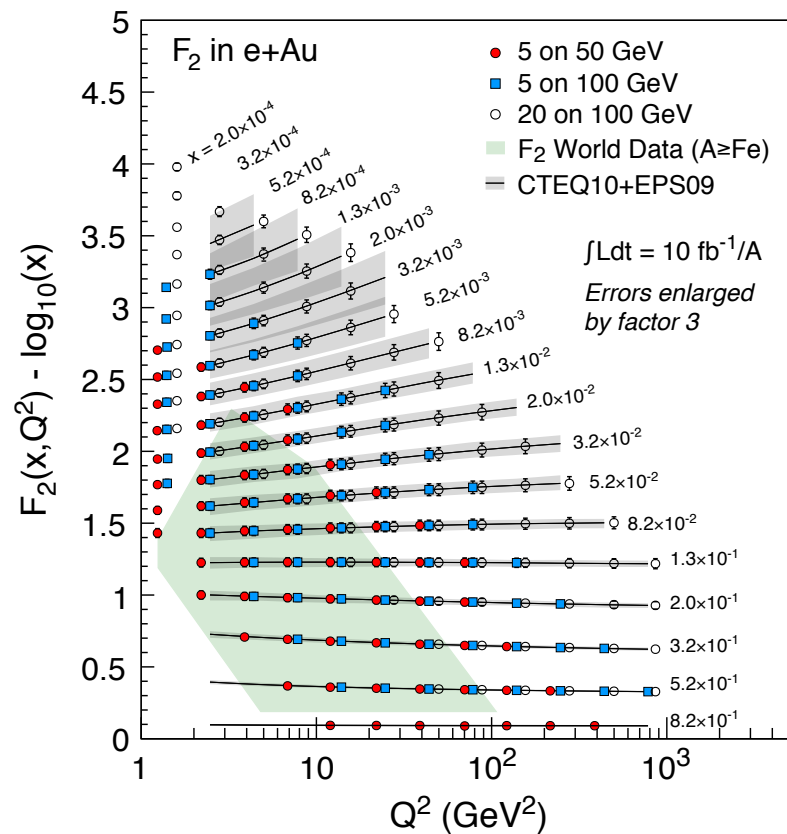
Correlated and uncorrelated systematics



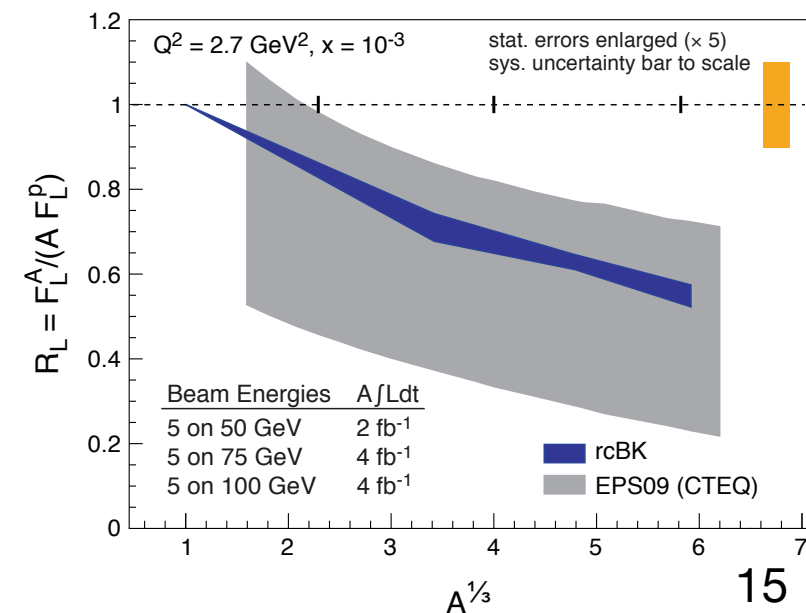
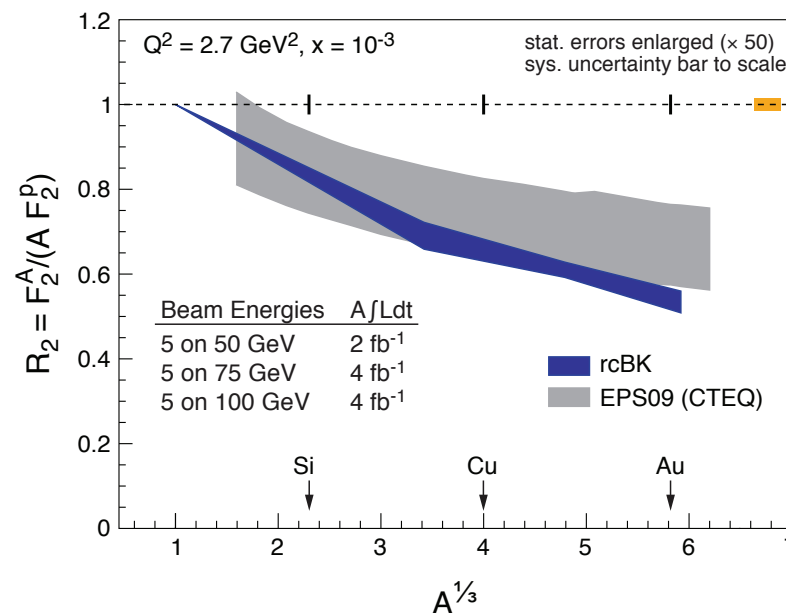
# Structure functions at EIC

## EIC: structure function simulations in eA

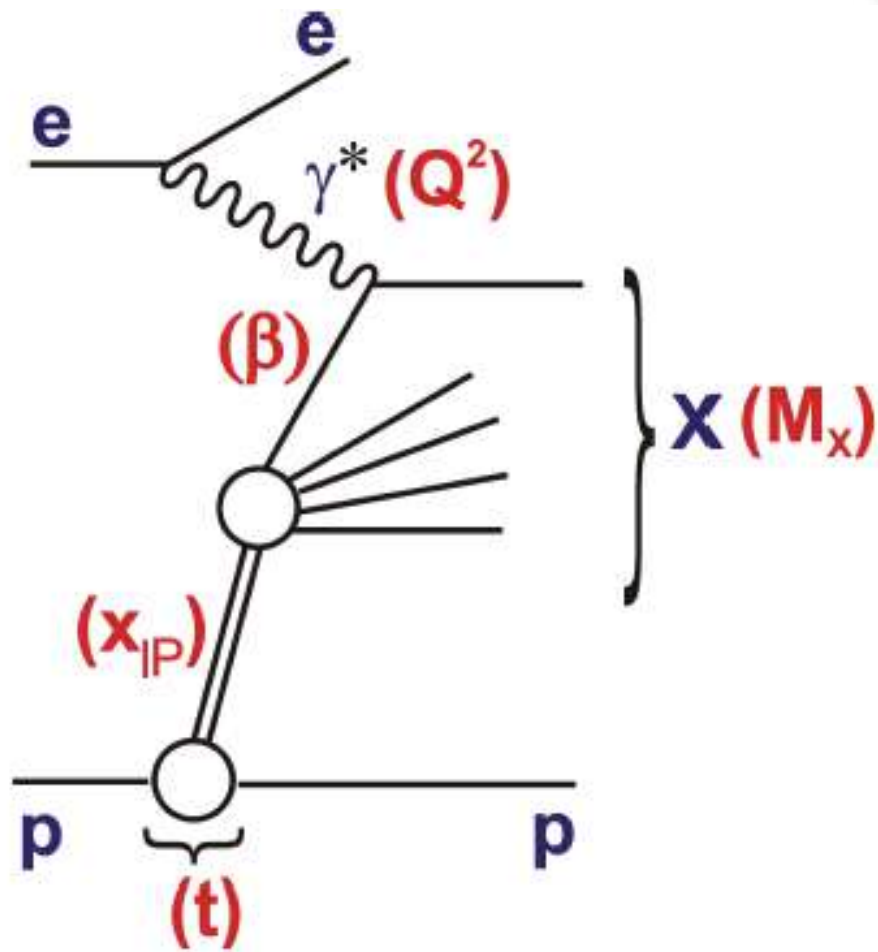
Pseudodata simulated with EPS09, very high precision data for eA



- Nonlinear evolution has smaller range of uncertainty. Robustness of the solution to nonlinear equation.
- Large dependence on the initial conditions for the linear evolution leads to large uncertainty.



# Diffraction



$$\xi \equiv x_{IP} = \frac{Q^2 + M_X^2 - t}{Q^2 + W^2}$$

momentum fraction of  
the Pomeron w.r.t  
hadron

$$\beta = \frac{Q^2}{Q^2 + M_X^2 - t}$$

momentum fraction  
of parton w.r.t  
Pomeron

$$x_{Bj} = x_{IP} \beta$$

Theoretical description of such process is in terms  
color-less exchange : the Pomeron.

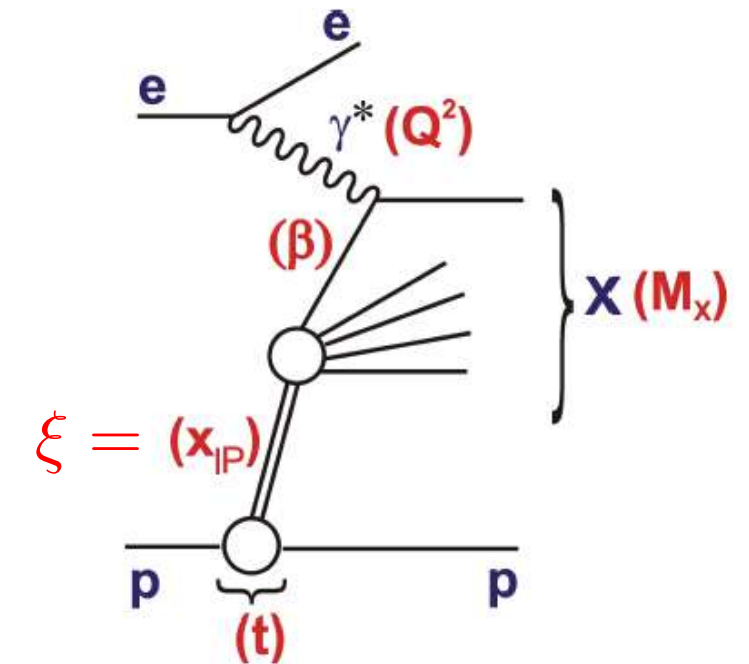
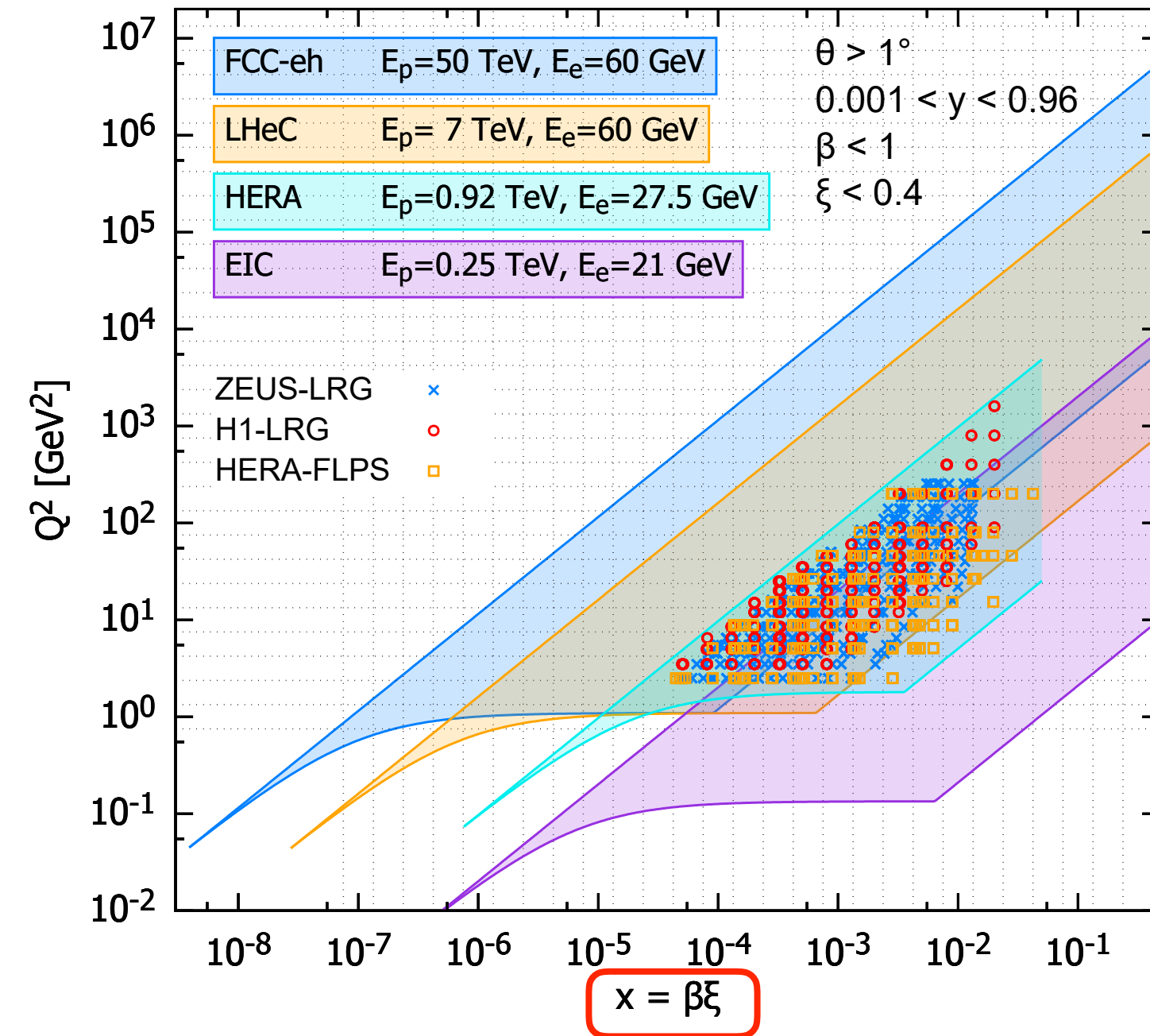
For large scales the QCD factorization was shown.

## What can be done at an EIC/LHeC/FCC-eh?

- Tests of **factorization** of diffractive parton distributions (ep and eA).
- Sensitivity and relation to **saturation** physics (smaller scales involved).
- Study relation between **diffraction** in ep and **shadowing** in eA.



# Phase space: LHeC, FCC-eh, EIC



$$E_e = 60 \text{ GeV}$$

LHeC

$E_p = 7 \text{ TeV}$  vs. HERA

- $x_{\min}$  down by factor  $\sim 20$
- $Q_{\max}^2$  up by factor  $\sim 100$

FCC

$E_p = 50 \text{ TeV}$  vs. 7 TeV

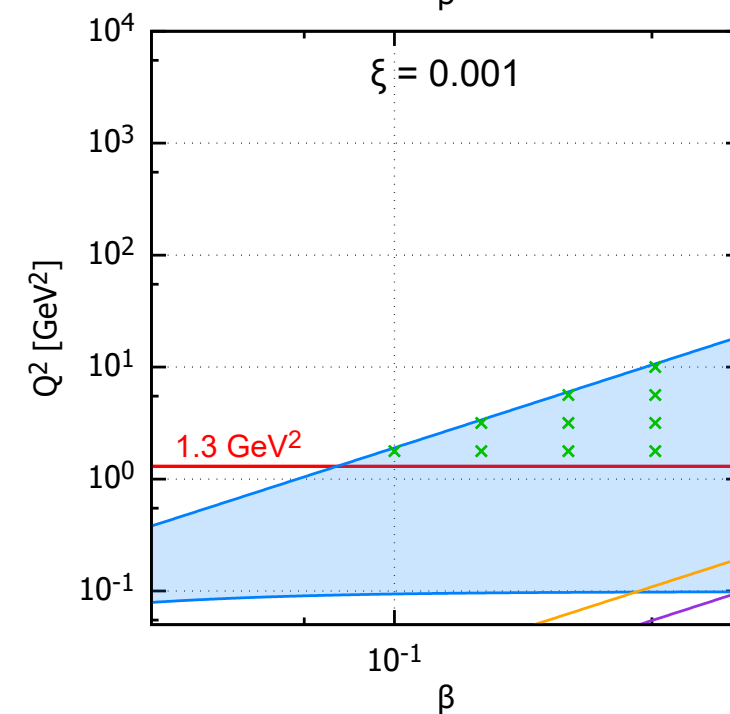
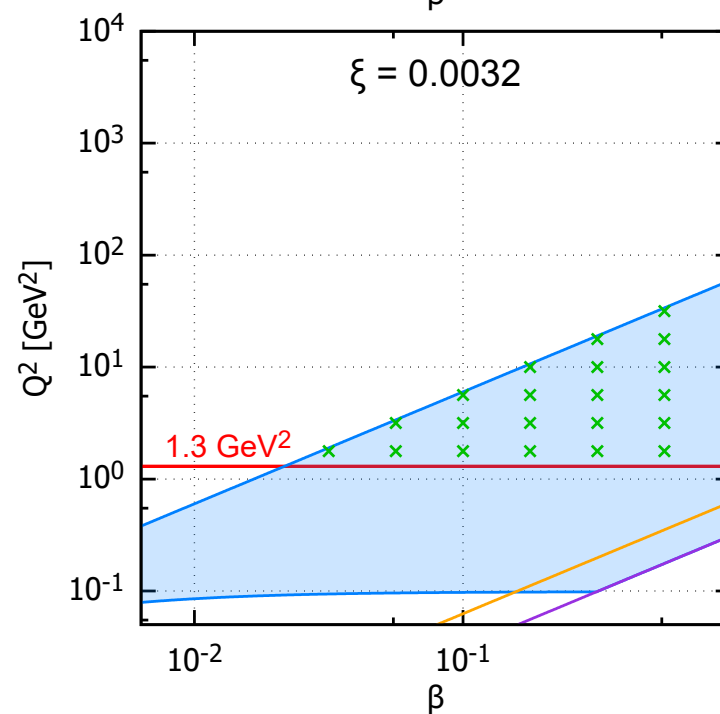
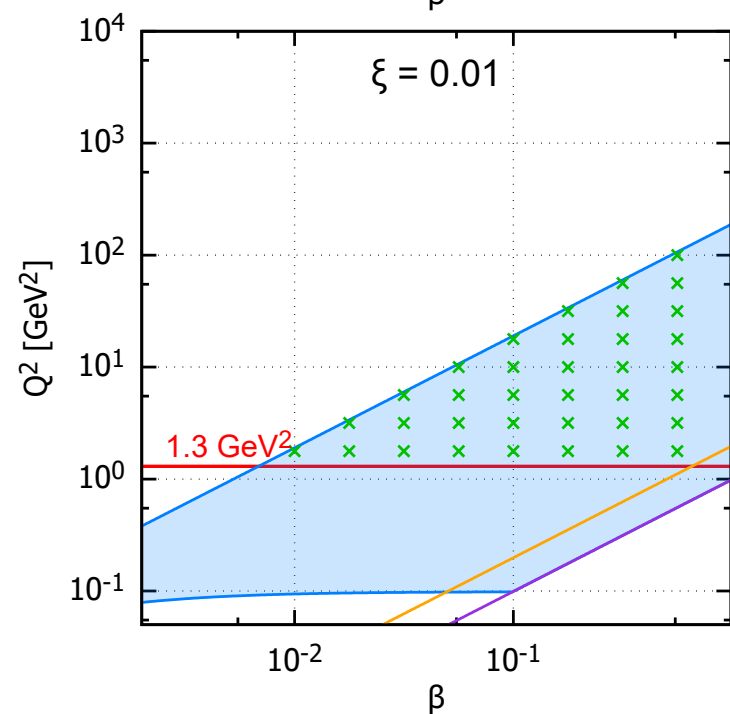
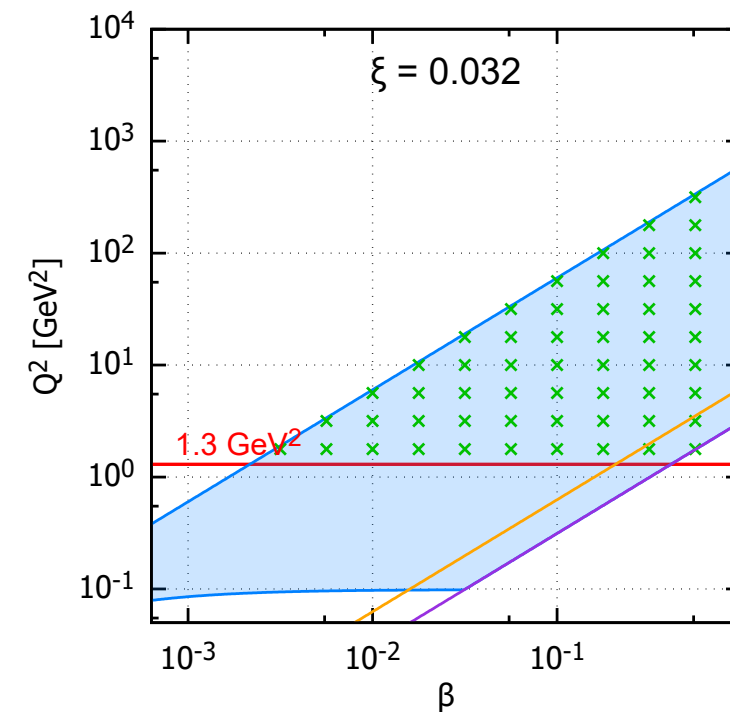
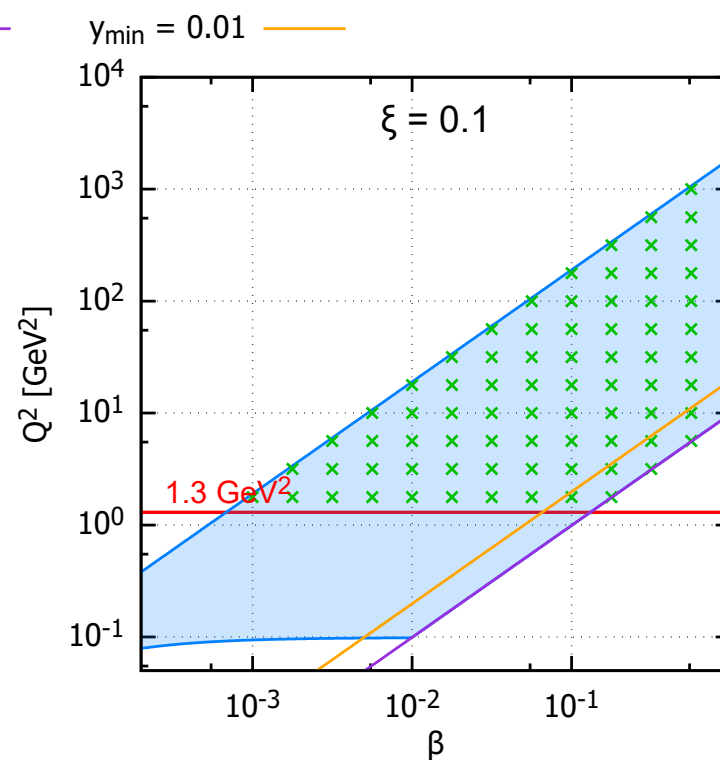
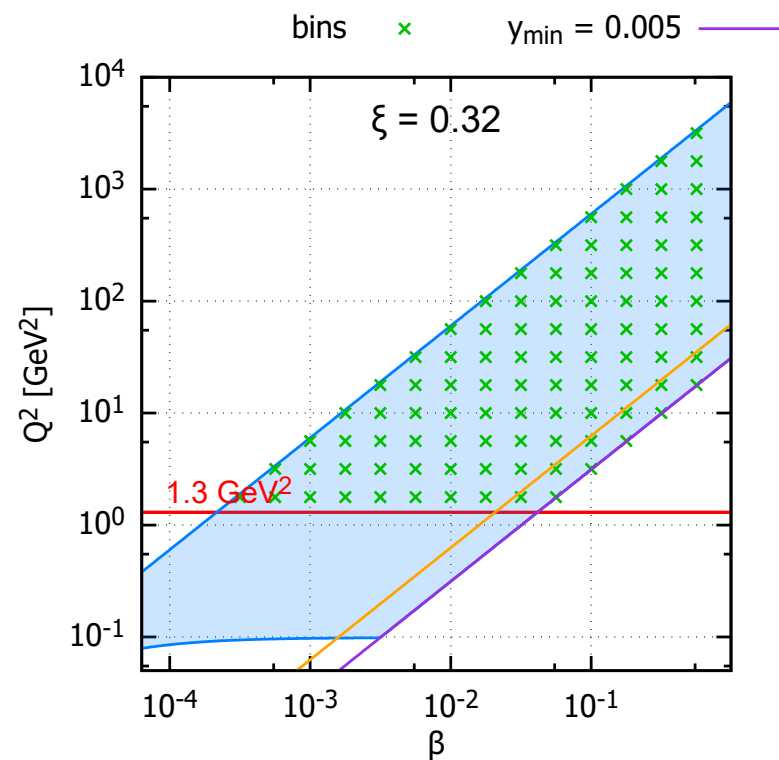
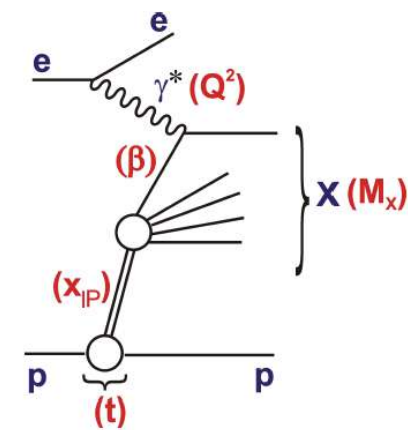
- $x_{\min}$  down by factor  $\sim 10$
- $Q_{\max}^2$  up by factor  $\sim 10$

For the EIC: better than HERA coverage of the large  $x$  region

# EIC phase space: $(\beta, Q^2)$ fixed $\xi$

$$\xi = x_{IP}$$

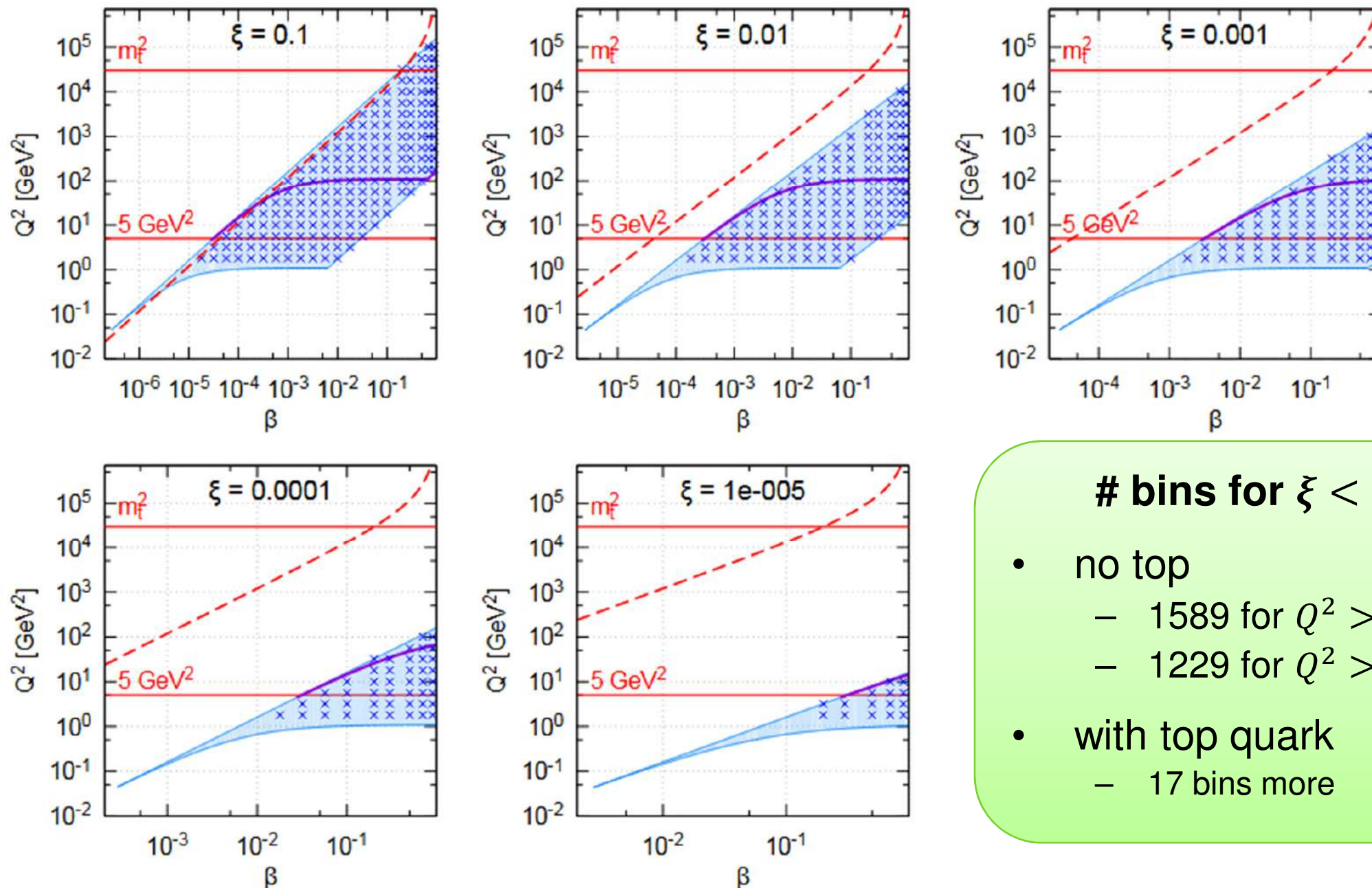
$$E_p = 275 \text{ GeV}, E_e = 18 \text{ GeV}, y_{\max} = 0.96$$



# LHeC phase space: $(\beta, Q^2)$ fixed $\xi$

$E_p = 7 \text{ TeV}$ ,  $E_e = 60 \text{ GeV}$ ,  $y_{\min} = 0.001$ ,  $y_{\max} = 0.96$

$\theta > 1^\circ$  ■  $\theta = 10^\circ$  — bins  $\times$   $M_X = 2 m_t$  - - -



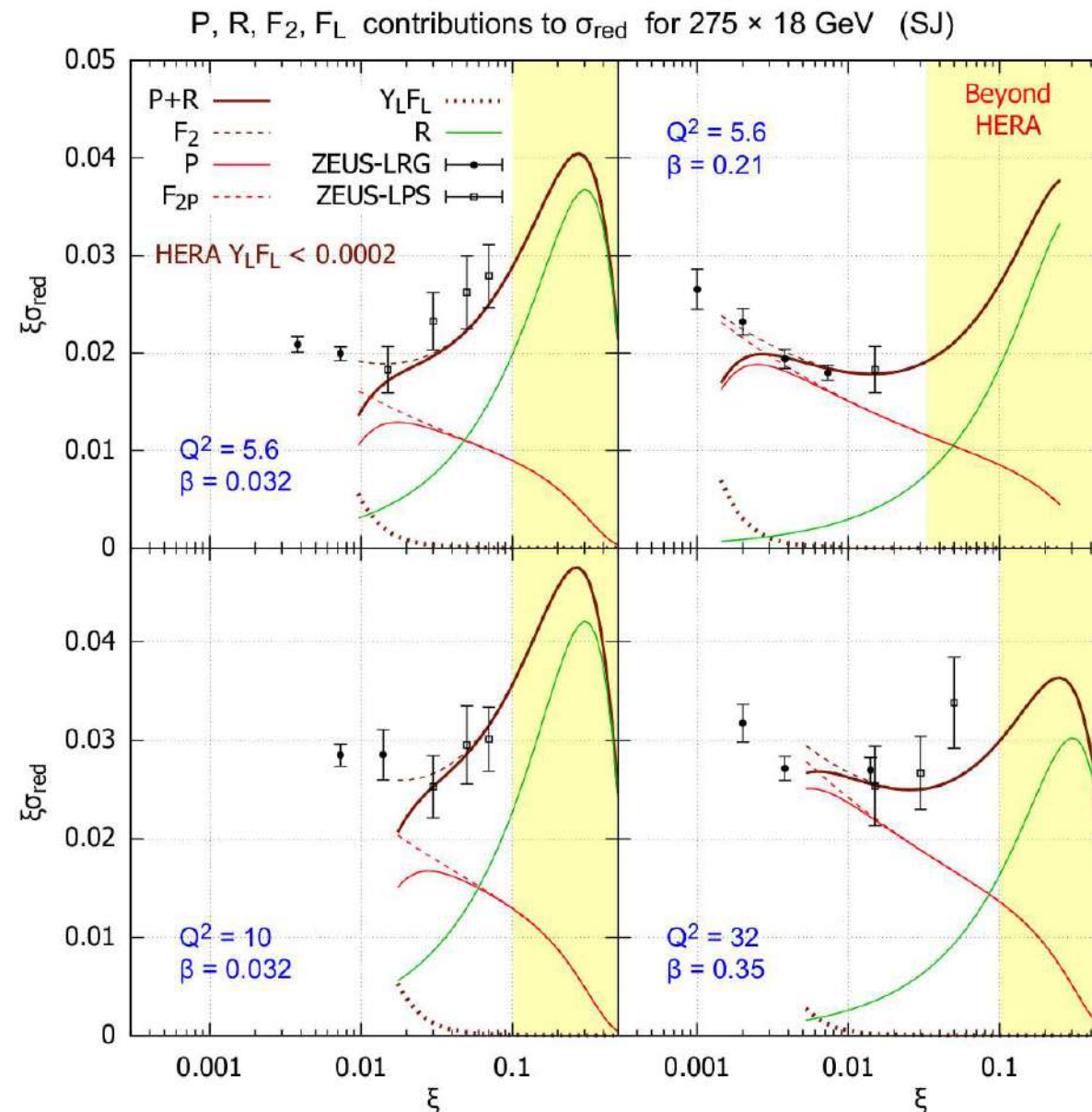
## # bins for $\xi < 0.15$

- no top
  - 1589 for  $Q^2 > 1.3 \text{ GeV}^2$
  - 1229 for  $Q^2 > 5 \text{ GeV}^2$
- with top quark
  - 17 bins more



# EIC: Pomeron/Reggeon decomposition

Pomeron, Reggeon,  $F_2$ ,  $F_L$  components of  $\sigma_{\text{red}}$



- ❑  $\mathcal{R}$  contribution dominates at high  $\xi$
- ❑ Significant  $F_L$  component

$$\sigma_{\text{red}} = F_2 - Y_L(y) F_L$$

$$Y_L(y) = \frac{y^2}{1 + (1 - y)^2}$$

At fixed  $(x, Q^2)$ ,  
 $Y_L(y)$  scales stronger than  $\sim 1/s^2$ ,  
 e.g.  $Y_L(0.9/5)/Y_L(0.9) = 0.024$

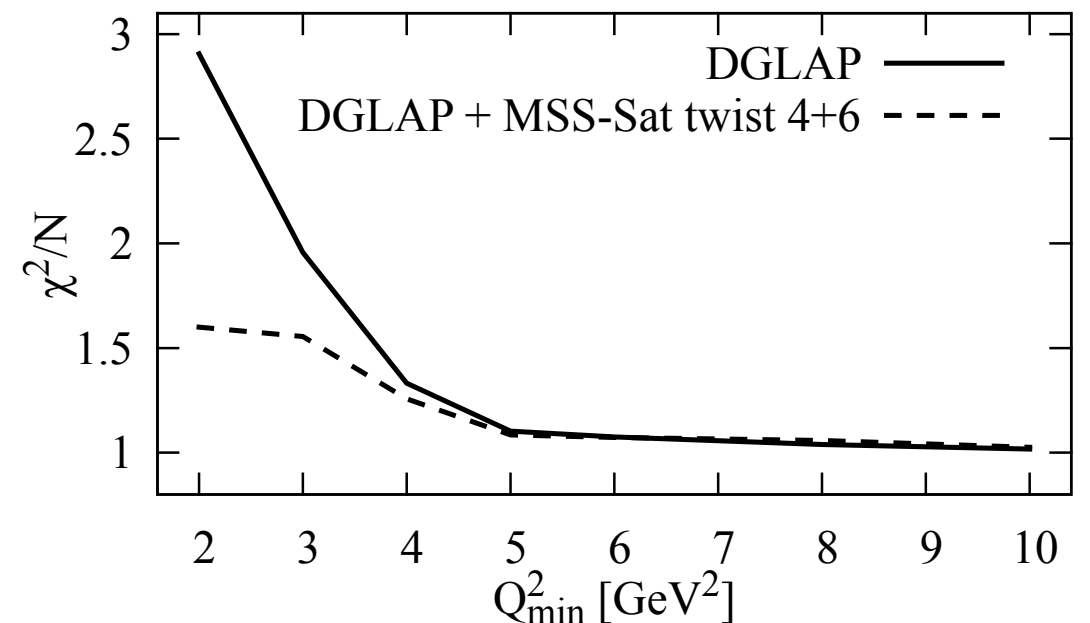
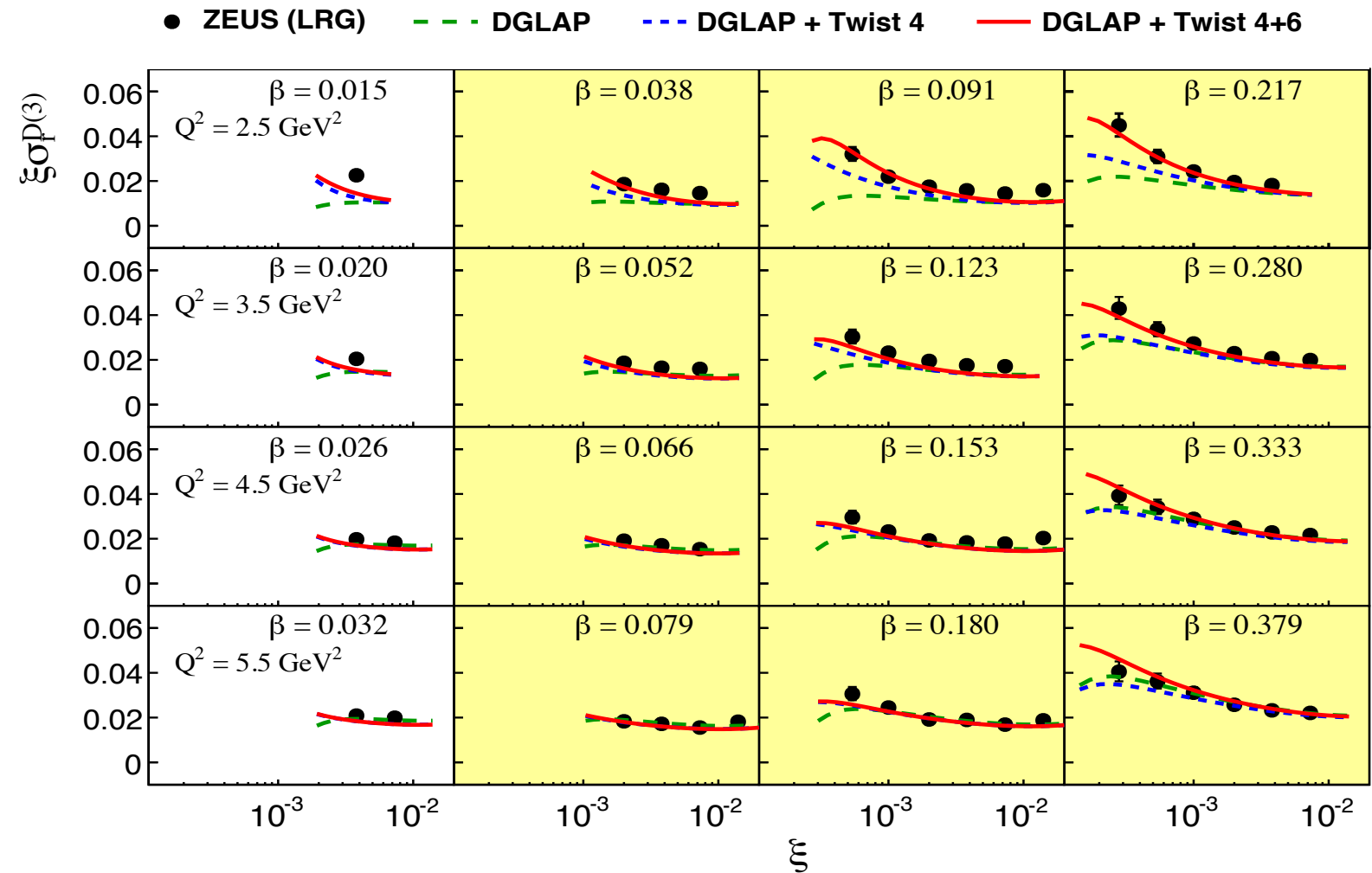
$x_L \lesssim 0.6$  required for the determination of subleading “Reggeon” term.  
 Some intermediate beam energy settings needed for  $F_L$  measurements.



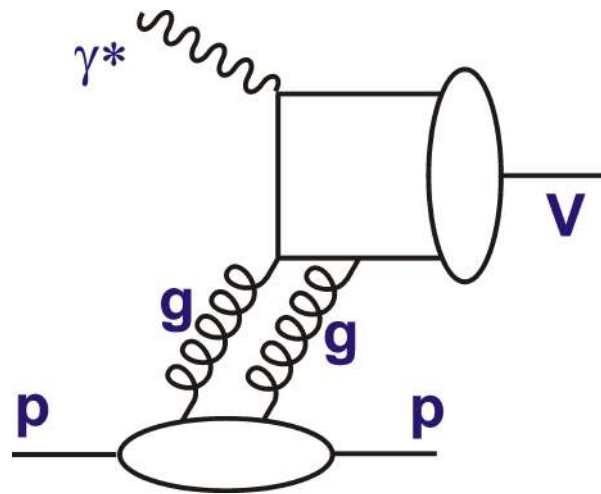
# Higher twists in diffraction

*Motyka, Sadzikowski, Slominski*

- Diffractive data at HERA cannot be described by DGLAP at low  $Q^2$
- Higher twists 4 and 6 evaluated from the dipole saturation model
- Improves the quality of the fit significantly
- Largest effect at low  $Q^2$  and small  $\xi$
- Indication for large higher twists
- Questions for EIC/LHeC/FCC-eh: how would that change with different  $A$  and energy?

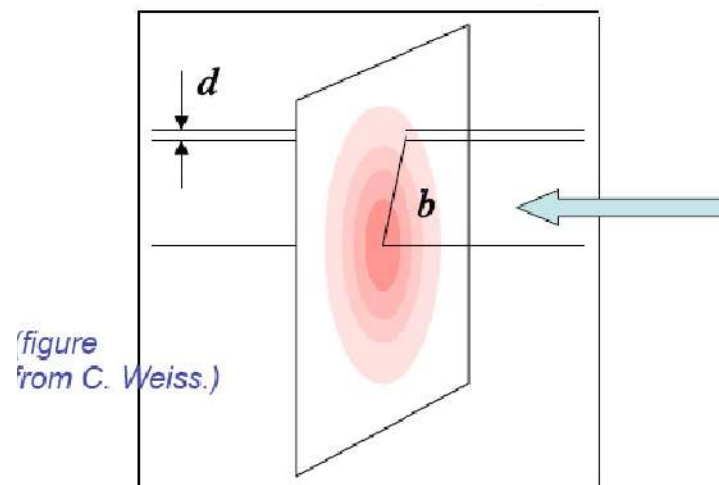
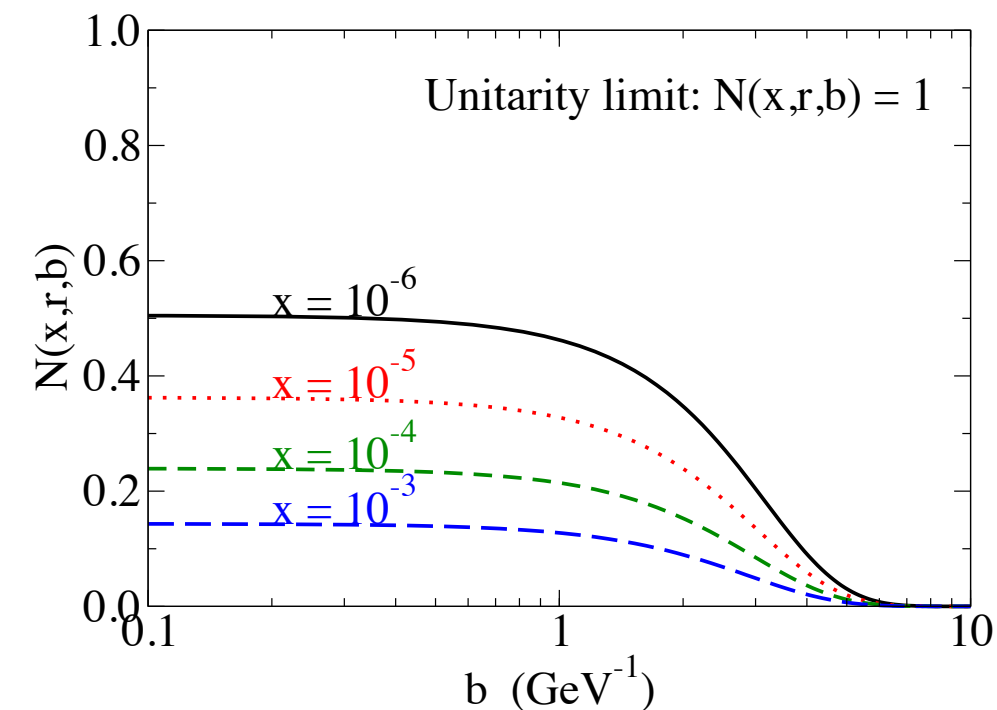


# Exclusive diffraction



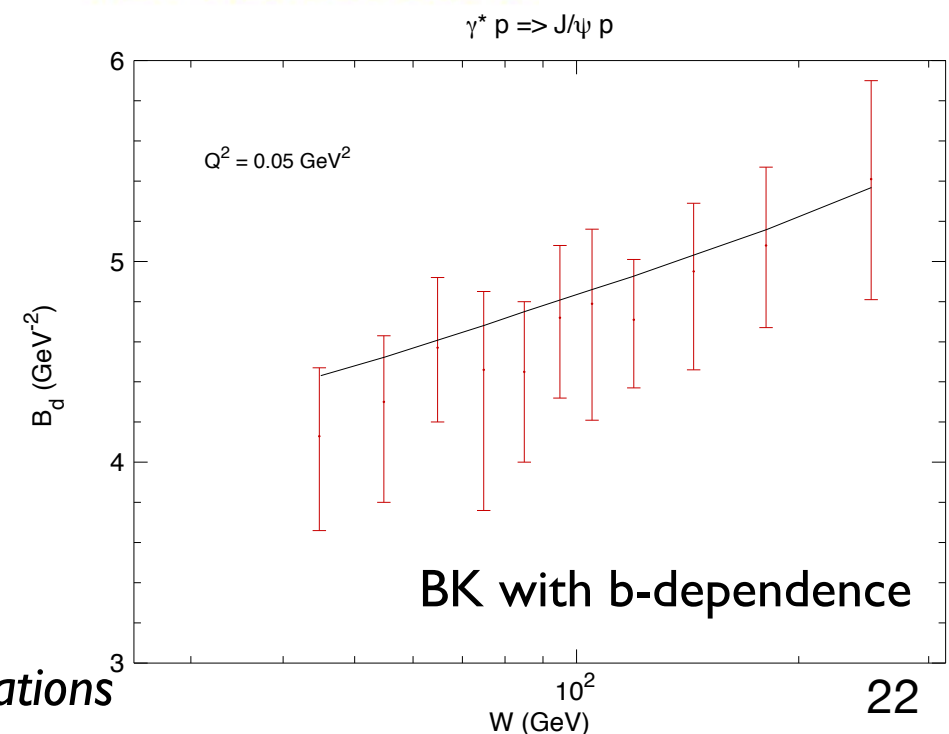
- Exclusive diffractive production of VM : extracting the dipole amplitude and GPDs
- Suitable process for estimating the 'blackness' of the interaction.
- $t$ -dependence : impact parameter profile

"b-Sat" dipole scattering amplitude with  $r = 1 \text{ GeV}^{-1}$



Central black region growing with decrease of  $x$ .

Large momentum transfer  $t$  probes small impact parameter where the density of interaction region is most dense.



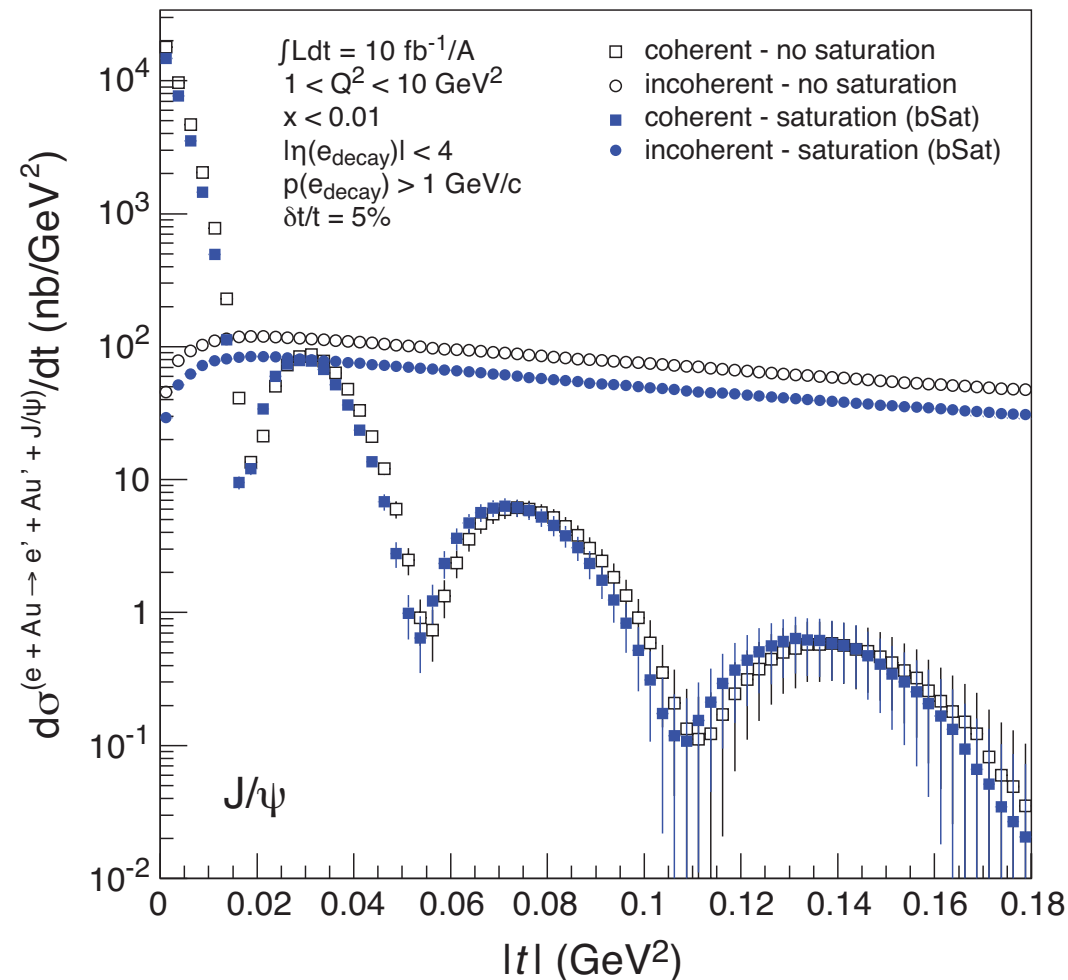
HERA data compared with nonlinear evolution simulations

# Exclusive diffraction on nuclei

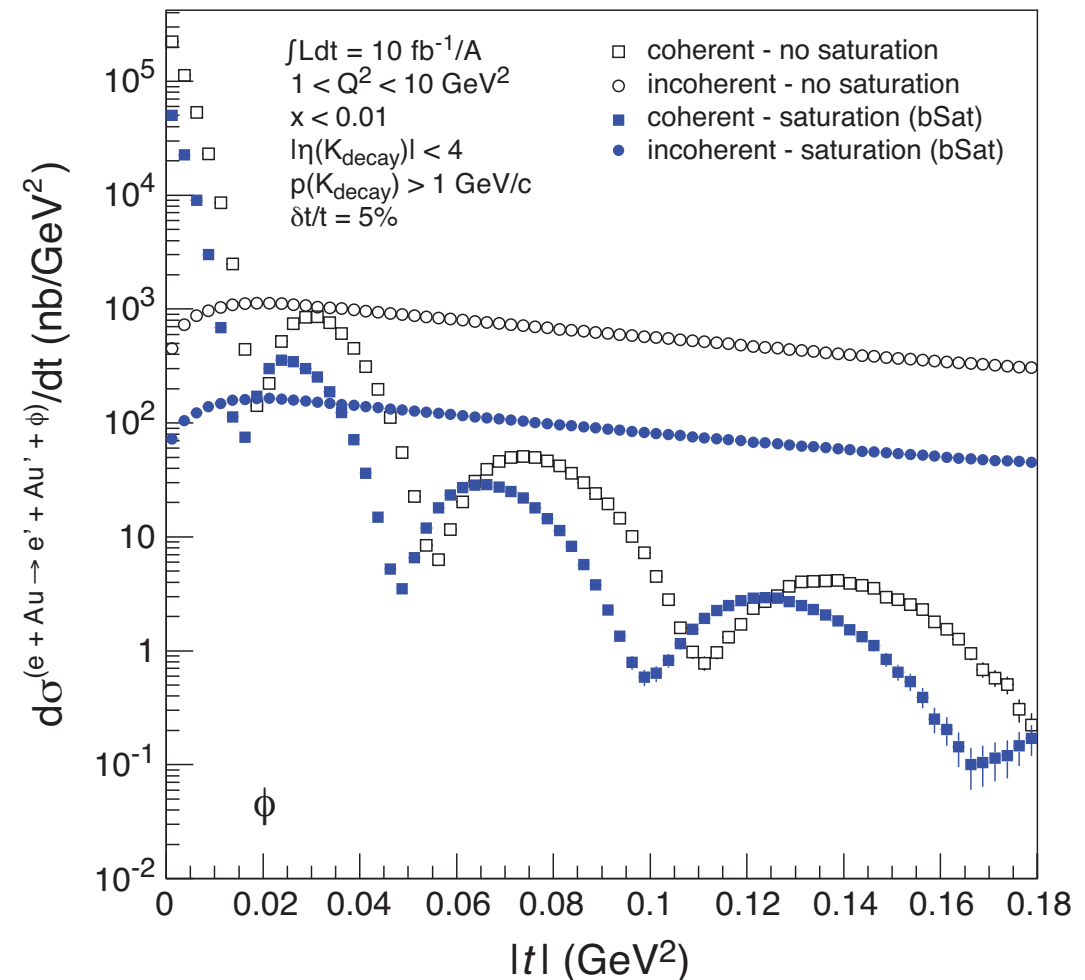
Possibility of using the same principle to learn about the gluon distribution in the nucleus.

Possible nuclear resonances at small  $t$ ?

## EIC: $J/\psi$



## EIC: $\phi$

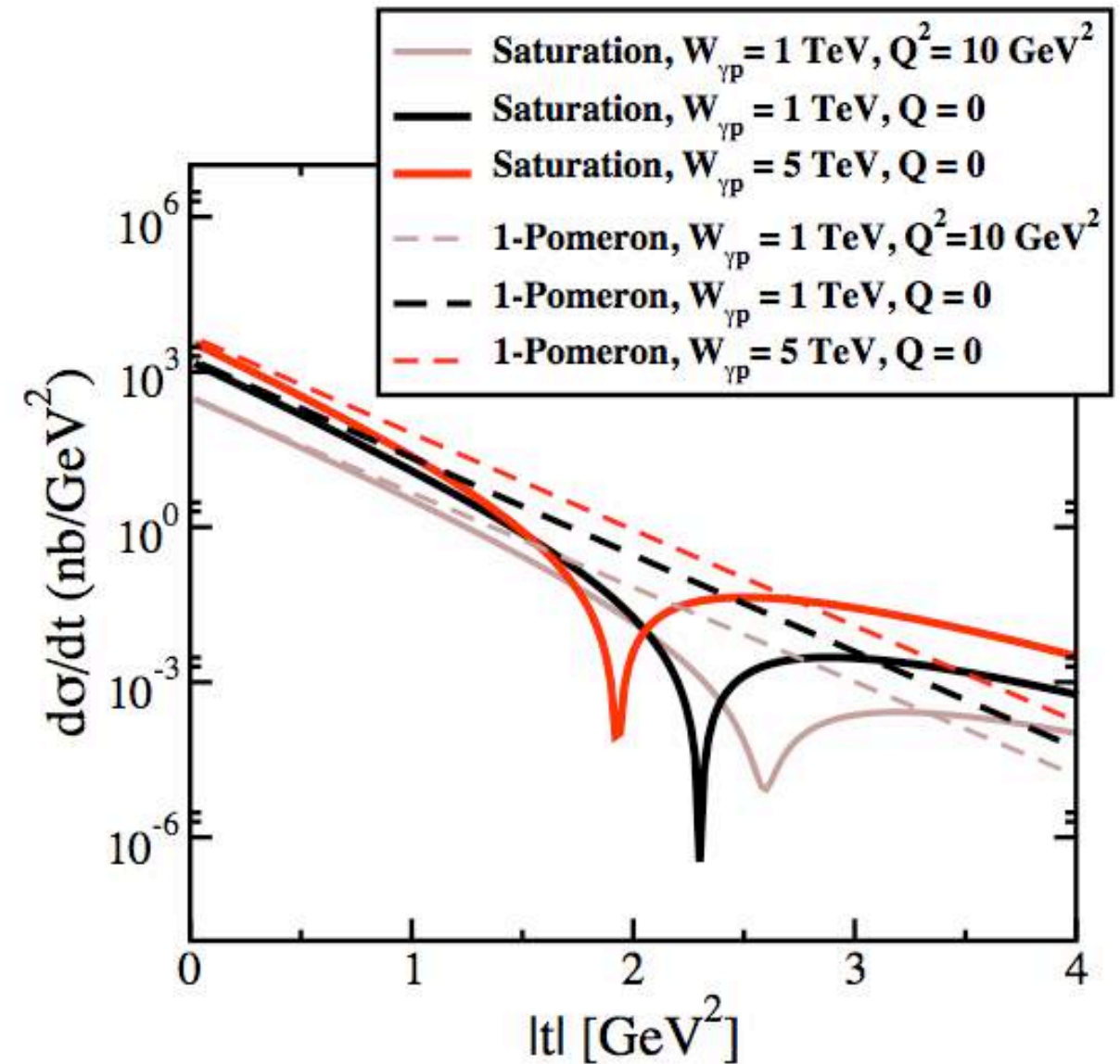
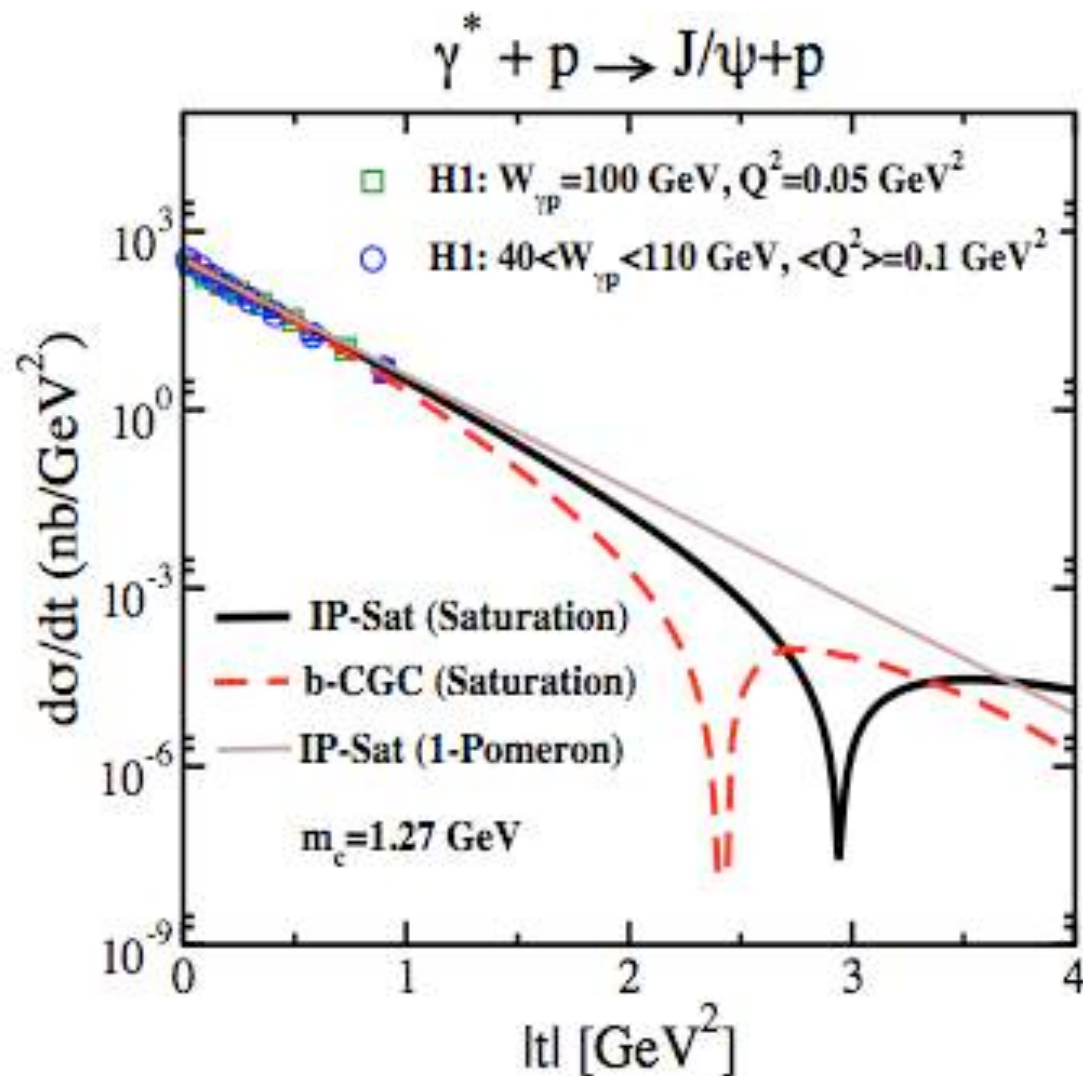


t-dependence: for nuclei dips. Position depends on model (sat no sat)

Challenges: need to distinguish between coherent and incoherent diffraction. Need dedicated instrumentation, zero degree calorimeter.

# Dips in t-profile for VM production

Armesto-Rezaeian



- t-dependence is a Fourier transform of the impact parameter profile
- characteristic dips as a feature of saturation
- position of dips depends on energy and scale
- within the LHeC sensitive t-range



# Summary

- Novel QCD phenomena expected at **high parton density**.
- Can reach this regime either by **increasing  $A$**  or **decreasing  $x$** .
- Proton and nuclear structure functions and PDFs can provide the test of these effects. Quantifying possible **deviations from DGLAP evolution**.
- **$F_L$**  measurement would greatly improve the prospects of constraining **higher twists** and **saturation**. Importance of heavy quark measurements.
- **Diffraction**, both inclusive and exclusive offers unique window to saturation physics. Relation between **diffraction and shadowing**. Inclusive data at HERA point to higher twists in this process. EIC can disentangle **Reggeon/Pomeron** contribution.
- **Exclusive diffraction** one of the best ways to perform the nucleon/nucleus tomography. VM elastic diffractive production; dips in  $t$  as a sign of parton saturation.
- **Incoherent diffraction** as a probe of the fluctuation of the gluon density.
- **Azimuthal (de)correlations**, sensitivity to the intrinsic transverse momentum of the gluon in the low  $x$  (or high  $A$ ) regime. **Ridge, collective** phenomena at ep/eA?
- Importance of **low  $x$**  dynamics to ultrahigh cosmic ray and neutrino physics (Auger, ICECUBE)